



University of Hradec Králové  
Faculty of Science

---

PROCEEDINGS OF  
*2<sup>nd</sup>* INTERNATIONAL PHYSICS DAYS  
of HRADEC KRÁLOVÉ 2023

Published on October 18, 2023

# 2<sup>nd</sup> Hradec Králové International PHYSICS DAYS



University of Hradec Králové  
**12 – 13 October 2023**

Conference Sections:  
Theoretical and Mathematical Physics  
Experimental and Applied Physics

## INFORMATION

The conference will be held in Hybrid form:

- Online attendance is free of charge
- In-person attendance fee is 2 500 CZK

**Deadline for registration and  
sending abstracts is 20<sup>th</sup>  
September**

Contact: [conference.ipd@uhk.cz](mailto:conference.ipd@uhk.cz)



## HONORARY CHAIR

Jan Kříž

Dean of the Faculty of Science  
University of Hradec Králové

## SCIENTIFIC COMMITTEE

Bilel Hamil (Algeria)  
Mustafa Moumni (Algeria)  
Andrii Khrabustovskyi (Czechia)  
Jiří Lipovský (Czechia)  
Bekir Can Lütfüoglu (Czechia)  
Jan Loskot (Czechia)  
Filip Studnička (Czechia)  
Jan Šlégr (Czechia)  
Miloslav Znojil (Czechia)  
Hassan Hassanabadi (Iran)  
Maciej Zubko (Poland)  
Erdoğan Ulas Saka (Turkey)

[uni.uhk.cz/ipd/](https://uni.uhk.cz/ipd/)

Hradec Králové International Physics Days 2023 Programme		
Time zone Prague time	12 October 2023 Thursday	
ONLINE-LIVE	Chairman: Bekir Can LUTFUOGLU	
08:00-08:15	Jan KRIZ	OPENNING TALK
08:20-08:45	Gurkan CELEBI	PHYSICS EDUCATION AND RESEARCH IN I.U.
08:50-09:15	Mustafa MOUMNI	EUP EFFECTS ON 3D DKP OSCILLATOR
09:20-09:45	Latevi LAWSON	STATISTICAL DESCRIPTIONS OF IDEAL GAS FROM POSITION DEFORMED NONCOMMUTATIVITY
ONLINE-LIVE	Chairman: Bekir Can LUTFUOGLU	
10:15-10:30	Karsten GLOWKA	MICROSTRUCTURE CHARACTERISTIC OF $(\text{TiTaNbZr})_{100-x}\text{Cu}_x$ HIGH ENTROPY ALLOYS FOR POTENTIAL ANTIBACTERIAL PROPERTIES
10:35-10:50	Deniz KAYA	CALCULATION OF PAIR CORRELATION FUNCTION IN GAS AND CRYSTAL PHASES OF TEMPERATURE SENSITIVE COLLOIDAL SYSTEM
10:55-11:10	Ulas SAKA	HOW TO CALCULATE BLACK HOLE SHADOW
11:15-11:30	Soroush ZARE	BUMBLEBEE BLACK HOLES SURROUNDED BY DARK MATTER SPIKE
11:35-11:50	Mahsaalsadet HOSSEINI	THE WEYL EQUATION IN THE SOM-RAYCHAUDHURI SPACE-TIME IN THE PRESENCE OF AN EXTERNAL ELECTROMAGNETIC FIELD
IN PERSON UHK 4th Floor Room 74060	Chairman: Filip STUDNIČKA	
13:30-13:55	Andrii KHRABUSTOVSKYI	NEUMANN SIEVE PROBLEM REVISITED
14:00-14:25	Miloslav ZNOJIL	QUANTUM GRAVITY VIA TWO WHEELER-DEWITT EQUATIONS
14:30-14:45	Jan LOSKOT	MICROANALYSES OF 3D-PRINTED PRODUCTS MADE OF THERMOPLASTICS BY THE HOT-MELT EXTRUSION METHOD
14:50-15:05	Marzieh BARADARAN	MAGNETIC QUANTUM GRAPHS WITH TIME-REVERSAL NON-INVARIANT VERTEX COUPLING
ONLINE-LIVE	Chairman: Ulas SAKA	
16:00-16:15	D. Kishore KUMAR	LOW-COST COPPER THIOCYANATE AS AN ALTERNATE HOLE-TRANSPORT MATERIAL FOR PEROVSKITE SOLAR CELLS
16:20-16:35	Bakhta CHERIFI	THE FACT OF MOTION IN DIPOLAR BEC
16:40-16:55	Fariba KAFIKANG	RADIUS OF THE WHITE DWARF ACCORDING TO FERMI ENERGY IN A $\delta^{\text{kappa}}$ -DEFORMED FRAMEWORK
17:00-17:15	Hadjar REZKI	NON-COMMUTATIVE KLEIN-GORDON EQUATION AND MECHANISM OF SCALAR PARTICLES PAIR PRODUCTION
17:20-17:35	Moussa ABBAD	A STUDY OF THE MOTION OF BOSON PARTICLES WITH INTERACTION IN THE COSMIC STRING SPACE TIME
17:40-17:55	Mouna BOUHELAL	SHELL-MODEL STUDY OF THE SPECTROSCOPIC PROPERTIES OF THE $\delta^{(26)}\text{Mg}$ AND $\delta^{(26)}\text{Si}$ MIRRORS
18:00-18:15	Fatima KOUDJIL	TRIPLE BOSE MIXTURES ON A SINGLE SPECIES
18:20-18:35	Abir SELIM	SHELL MODEL DESCRIPTION OF THE $\delta^{(24)}\text{Al}-\delta^{(24)}\text{Na}$ MIRRORS STRUCTURE
Hradec Králové International Physics Days 2023 Programme		
Time zone Prague time	13 October 2023 Friday	
Pre-recorded	Chairman: ULAS SAKA	
08:00-08:15	Fateh MERABTINE	BOSE GAS OF A QUASI TWO-DIMENSIONAL HARMONICALLY TRAPPED IN THE DUNKL ALGEBRA
08:15-08:30	Atika MEHEDI	CORRELATIONS IN 1D HOMOGENEOUS BOSE MIXTURES
08:30-08:45	Zohra MEHRI	EXPANSION A 3D DIPOLAR BEC IN RANDOM POTENTIALS
08:45-09:00	Amenallah ANDOLSI	THE PLANNER VECTOR DKP OSCILLATOR WITH MINIMAL LENGTH
09:00-09:15	Lakhdar SEK	DUFFIN KEMMER PETIAU OSCILLATOR IN A UNIFORM MAGNETIC FIELD IN ANTI de SITTER SPACE
09:15-09:30	Meriem ABDELAZIZ	APPROXIMATE SOLUTIONS OF THE ROSEN-MORSE POTENTIAL BY MEANS OF THE NIKIFOROV-UVAROV METHOD
09:30-09:45	Zeyneb TAIBI	SOLITON SOLUTION OF GROSS-PITAEVSKII EQUATION
09:45-10:00	Karima ABBAS	QUANTUM LIQUID DROPLETS IN BOSE MIXTURES WITH WEAK DISORDER
Pre-recorded	Chairman: ULAS SAKA	
11:00-11:15	Asma MERAD	THE KIEIN-GORDON OSCILLATOR IN THE PRESENCE OF A MINIMAL LENGTH
11:15-11:30	Pawel ŚWIEC	NANOCRYSTALLINE NITI ALLOYS PRODUCED BY COLD ROLLING IN THE MARTENSITIC STATE
11:30-11:45	Muzaffer ERDOGAN	CALCULATION OF SELF INDUCTANCE OF A FINITE COIL
11:45-12:00	M'hamed HADJ MOUSSA	SOLUTION OF THE DUFFIN-KEMMER-PETIAU EQUATION IN SNYDER-DE SITTER SPACE
12:00-12:15	Mohamed Walid HALIMI	POSITRON ANNIHILATION LIFETIME SPECTROSCOPY MEASUREMENTS USING Na-22 POSITRON RADIO-ISOTOPE
12:15-12:30	Ali ASKARI	SCATTERING AND BOUND STATES FOR THE COULOMB POTENTIAL WITH DUNKL OPERATOR IN 3 - DIMENSIONS
12:30-12:45	Narges HEIDARI	EXPLORING THE EFFECT OF GUP ON SCATTERING OF SCHWARZSCHILD BLACK HOLE
12:45-13:00	Bekir Can LUTFUOGLU	AN ANALYSIS ON THE THERMAL QUANTITIES OF QUANTUM-CORRECTED SCHWARZSCHILD ADS BLACK HOLE SURROUNDED BY QUINTESSENCE MATTER
Closing Talk		

# Contents

<b>Contribution 1</b>	<b>1</b>
1.1 Abir SELIM et al. SHELL MODEL DESCRIPTION OF THE $^{24}\text{Al}$ - $^{24}\text{Na}$ MIRRORS STRUCTURE . . . . .	1
<b>Contribution 2</b>	<b>3</b>
2.1 Ali ASKARI et al. SCATTERING AND BOUND STATES FOR THE COULOMB POTENTIAL WITH DUNKL OPERATOR IN 3 - DIMENSIONS . . . . .	3
<b>Contribution 3</b>	<b>5</b>
3.1 Amenallah ANDOLSI et al. THE PLANNER VECTOR DKP OSCILLATOR WITH MINIMAL LENGTH . . . . .	5
<b>Contribution 4</b>	<b>6</b>
4.1 Andrii KHRABUSTOVSKYI NEUMANN SIEVE PROBLEM REVISITED . . . . .	6
<b>Contribution 5</b>	<b>7</b>
5.1 Asma MERAD THE KLEIN-GORDON OSCILLATOR IN THE PRESENCE OF A MINIMAL LENGTH . . . . .	7
<b>Contribution 6</b>	<b>8</b>
6.1 Atika MEHEDI et al. CORRELATIONS IN 1D HOMOGENEOUS BOSE MIXTURES . . . . .	8
<b>Contribution 7</b>	<b>9</b>
7.1 Bakhta CHERIFI et al. THE FACT OF MOTION IN DIPOLAR BEC . . . . .	9

<b>Contribution 8</b>	<b>10</b>
8.1 Bekir Can LUTFUOGLU et al. AN ANALYSIS ON THE THERMAL QUANTITIES OF QUANTUM-CORRECTED SCHWARZSCHILD ADS BLACK HOLE SURROUNDED BY QUINTESSENCE MATTER . . . . .	10
<b>Contribution 9</b>	<b>11</b>
9.1 Deniz KAYA CALCULATION OF PAIR CORRELATION FUNCTION IN GAS AND CRYSTAL PHASES OF TEMPERATURE SENSITIVE COLLOIDAL SYSTEM . . . . .	11
<b>Contribution 10</b>	<b>18</b>
10.1 Fariba KAFIKANG et al. RADIUS OF THE WHITE DWARF ACCORDING TO FERMI ENERGY IN A $\kappa$ -DEFORMED FRAMEWORK . . . . .	18
<b>Contribution 11</b>	<b>19</b>
11.1 Fateh MERABTINE et al. BOSE GAS OF A QUASI TWO-DIMENSIONAL HARMONICALLY TRAPPED IN THE DUNKL ALGEBRA . . . . .	19
<b>Contribution 12</b>	<b>21</b>
12.1 Fatima KOUDJIL et al. TRIPLE BOSE MIXTURES ON A SINGLE SPECIES . . . . .	21
<b>Contribution 13</b>	<b>22</b>
13.1 Gürkan ÇELEBİ PHYSICS EDUCATION and RESEARCH IN I. U. . . . .	22
<b>Contribution 14</b>	<b>23</b>
14.1 Hadjar REZKI et al. NON-COMMUTATIVE KLEIN-GORDON EQUATION AND MECHANISM OF SCALAR PARTICLES PAIR PRODUCTION . . . . .	23
<b>Contribution 15</b>	<b>24</b>
15.1 Jan LOSKOT MICROANALYSES OF 3D-PRINTED PRODUCTS MADE OF THERMOPLASTICS BY THE HOT-MELT EXTRUSION METHOD . . . . .	24

<b>Contribution 16</b>	<b>25</b>
16.1 Karima ABBAS et al. QUANTUM LIQUID DROPLETS IN BOSE MIXTURES WITH WEAK DISORDER . . . . .	25
<b>Contribution 17</b>	<b>27</b>
17.1 Karsten GLOWKA et al. MICROSTRUCTURE CHARACTERISTIC OF $(TiTaNbZr)_{100-x}Cu_x$ HIGH ENTROPY ALLOYS FOR POTENTIAL ANTIBACTERIAL PROPERTIES	27
<b>Contribution 18</b>	<b>29</b>
18.1 Kishore KUMAR LOW-COST COPPER THIOCYANATE AS AN ALTERNATE HOLE- TRANSPORT MATERIAL FOR PEROVSKITE SOLAR CELLS . . . . .	29
<b>Contribution 19</b>	<b>30</b>
19.1 Lakhdar SEK DUFFIN KEMMER PETIAU OSCILLATOR IN A UNIFORM MAG- NETIC FIELD IN ANTI de SITTER SPACE . . . . .	30
<b>Contribution 20</b>	<b>31</b>
20.1 Latévi M. LAWSON STATISTICAL DESCRIPTIONS OF IDEA GAS FROM POSITION DE- FORMED NONCOMMUTATIVITY . . . . .	31
<b>Contribution 21</b>	<b>33</b>
21.1 Mahsaalsadat HOSSEINI et al. THE WEYL EQUATION IN THE SOM-RAYCHAUDHURI SPACE-TIME IN THE PRESENCE OF AN EXTERNAL ELECTROMAGNETIC FIELD	33
<b>Contribution 22</b>	<b>35</b>
22.1 Marzieh BARADARAN MAGNETIC QUANTUM GRAPHS WITH TIME-REVERSAL NON- INVARIANT VERTEX COUPLING . . . . .	35
<b>Contribution 23</b>	<b>36</b>
23.1 Meriem ABDELAZIZ et al. APPROXIMATE SOLUTIONS OF THE ROSEN-MORSE POTENTIAL BY MEANS OF THE NIKIFOROV-UVAROV METHOD . . . . .	36

<b>Contribution 24</b>	<b>37</b>
24.1 M'hamed HADJ MOUSSA SOLUTION OF THE DUFFIN-KEMMER-PETIAU EQUATION IN SNYDER- DE SITTER SPACE . . . . .	37
<b>Contribution 25</b>	<b>38</b>
25.1 Miloslav ZNOJIL QUANTUM GRAVITY VIA TWO WHEELER-DEWITT EQUATIONS .	38
<b>Contribution 26</b>	<b>41</b>
26.1 Mohamed Walid HALIMI et al. POSITRON ANNIHILATION LIFETIME SPECTROSCOPY MEASURE- MENTS USING Na-22 POSITRON RADIO-ISOTOPE . . . . .	41
<b>Contribution 27</b>	<b>43</b>
27.1 Mouna BOUHELAL et al. SHELL-MODEL STUDY OF THE SPECTROSCOPIC PROPERTIES OF THE $^{26}\text{Mg}$ AND $^{26}\text{Si}$ MIRRORS . . . . .	43
<b>Contribution 28</b>	<b>45</b>
28.1 Moussa ABBAD et al. A STUDY OF THE MOTION OF BOSON PARTICLES WITH INTER- ACTION IN THE COSMIC STRING SPACE TIME . . . . .	45
<b>Contribution 29</b>	<b>46</b>
29.1 Mustafa MOUMNI et al. EUP EFFECTS ON 3D DKP OSCILLATOR . . . . .	46
<b>Contribution 30</b>	<b>48</b>
30.1 Muzaffer ERDOGAN CALCULATION OF SELF INDUCTANCE OF A FINITE COIL . . . . .	48
<b>Contribution 31</b>	<b>49</b>
31.1 Narges HEIDARI et al. EXPLORING THE EFFECT OF GUP ON SCATTERING OF SCHWARZSCHILD BLACK HOLE . . . . .	49
<b>Contribution 32</b>	<b>50</b>
32.1 Paweł ŚWIEC et al. NANOCRYSTALLINE NiTi ALLOYS PRODUCED BY COLD ROLLING IN THE MARTENSITIC STATE . . . . .	50

<b>Contribution 33</b>	<b>52</b>
33.1 Soroush ZARE et al. BUMBLEBEE BLACK HOLES SURROUNDED BY DARK MATTER SPIKE . . . . .	52
<b>Contribution 34</b>	<b>54</b>
34.1 Ulaş SAKA HOW TO CALCULATE BLACKHOLE SHADOW . . . . .	54
<b>Contribution 35</b>	<b>55</b>
35.1 Zeyneb TAIBI et al. SOLITON SOLUTION OF GROSS-PITAIEVSKII EQUATION . . . . .	55
<b>Contribution 36</b>	<b>56</b>
36.1 Zohra MEHRI et al. EXPANSION A 3D DIPOLAR BEC IN RANDOM POTENTIALS . . . . .	56



## SCIENTIFIC BOARD

- Bilel Hamil (Algeria)
- Moustafa Moumni (Algeria)
- Andrii Khrabustovskyi (Czechia)
- Jiří Lipovský (Czechia)
- Bekir Can Lütfüoglu (Czechia)
- Jan Loskot (Czechia)
- Filip Studnička (Czechia)
- Jan Šlégr (Czechia)
- Miloslav Znojil (Czechia)
- Hassan Hassanabadi (Iran)
- Maciej Zubko (Poland)
- Erdinç Ulaş Saka (Turkey)

## LOCAL ORGANIZATION COMMITTEE

- Bekir Can Lütfüoglu (Czechia)
- Jan Loskot (Czechia)
- Filip Studnička (Czechia)

The scientific board would like to thank Ulaş Saka for technical support.

# SHELL MODEL DESCRIPTION OF THE $^{24}\text{Al}$ - $^{24}\text{Na}$ MIRRORS STRUCTURE

Abir **SELIM**

LPAT, Faculty of exact Sciences, Natural Sciences and Life, Echahid Cheikh Larbi Tebessi University  
12000, Tebessa, Algeria  
*abirslm95@gmail.com*

Mouna **BOUHELAL**

LPAT, Faculty of exact Sciences, Natural Sciences and Life, Echahid Cheikh Larbi Tebessi University  
12000, Tebessa, Algeria  
*m.bouhelal@yahoo.fr*

Florent **HAAS**

*IPHC, University of Strasbourg*  
F-67037 Strasbourg, Cedex2, France

## Abstract

In recent years, there has been much experimental and theoretical work on the structure of nuclei close to the valley of stability, such as the sd shell nuclei region. Among the sd shell nuclei, the properties of the protonrich nuclei constitute a major challenge in nuclear astrophysical processes. In rp-process nucleosynthesis, the proton-rich  $^{24}\text{Al}$  is reached through the  $^{23}\text{Mg}(p, \gamma)^{24}\text{Al}$  reaction as well as the  $^{22}\text{Mg}(p, \gamma)^{23}\text{Al}(p, \gamma)^{24}\text{Si}(\beta)^{24}\text{Al}$  reaction chain [1].

The updated experimental spectrum of  $^{24}\text{Al}$  has been reported recently in Ref. [2]. All states above the proton threshold, 1.86 MeV, have either uncertain or unknown  $J^\pi$  assignments. In order to confirm the proposed spin/parity assignments and to determine the unknown ones, a comparison with shell-model calculation and with the mirror nucleus  $^{24}\text{Na}$  is crucial. We performed a shell-model calculation using the  $(0 + 1) \hbar\omega$  *PSDPF* interaction [3] and Nathan code [4] to calculate the excitation energy spectrum of  $^{24}\text{Al}$  up to 5 MeV, which includes the range above the proton threshold that is important for the astrophysical applications [5]. The comparison of our results, energy spectrum, and electromagnetic transitions, with their experiment and with their counterparts in  $^{24}\text{Na}$  will be presented in this contribution.

## References

- [1] N. Gerken et al., Phys. Rev. C **104**, 065807 (2021).
- [2] M.S.Basunia and A.Chakraborty, Nucl. Data Sheets **186**, 3 (2022) and <http://www.nndc.bnl.gov/nudat2/>.
- [3] M. Bouhelal, Ph.D. thesis, under joint supervision of University of Batna, Algeria, and University of Strasbourg, France (2010) and M. Bouhelal et al., Nucl. Phys. A **864**, 113 (2011).
- [4] E. Caurier, F. Nowacki, Acta Phys. Pol. B **30**, 705 (1999) and E. Caurier et al., Phys. Rev. C **59**, 2033 (1999).
- [5] L. Erikson et al., Phys. Rev. C **81**, 045808 (2010).

# SCATTERING AND BOUND STATES FOR THE COULOMB POTENTIAL WITH DUNKL OPERATOR IN 3 - DIMENSIONS

Ali **ASKARI**

Faculty of Physics, Shahrood University of Technology  
3619995161-316, Shahrood, Iran  
aliaskari@shahroodut.ac.ir

Hassan **HASSANABADI**

Faculty of Physics, Shahrood University of Technology  
3619995161-316, Shahrood, Iran  
0000-0001-7487-6898  
hha1349@gmail.com

Won-Sang **CHUNG**

Department of Physics and Research Institute of Natural Science, College of Natural Science, Gyeongsang National  
University, 660-701, Jinju, Korea  
0000-0002-1358-6384  
mimip44@naver.com

## Abstract

In this paper, our aim is to explore the phase shift resulting from Coulomb scattering within the framework of the Dunkl operator applied to a non-relativistic system. To accomplish this, we will solve the Schrödinger equation in three dimensions, taking into account both the Dunkl operator and the Coulomb potential. Our solutions will be expressed in the form of Hypergeometric functions. Subsequently, we will assess the behavior of these solutions as the system approaches its limiting state, allowing us to compute the phase shift caused by scattering. Furthermore, we will investigate the influence of the  $\mu$ -deform parameter on the phase shift and, consequently, on the wave function

## References

- [1] H. Hassanabadi, H. Sobhani, A. Banerjee, Eur. Phys. J. C **77**, 581 (2017).
- [2] A. Askari, H. Hassanabadi, W. S. Chung **38**, 21 (2023).

- [3] Ch. F. Dunkl. Mathematische Zeitschrift, 197(1), 3360 (1988).
- [4] A.I. Ahmadov, S.M. Aslanova, M. Sh. Orujova, S. V. Badalov , S.-H. Dong, Phys. Lett. A **383**, 3010 (2019).

# THE PLANNER VECTOR DKP OSCILLATOR WITH MINIMAL LENGTH

Amenallah **ANDOLSI**

Unit of Nuclear and High Energy Physics, Faculty of Sciences of Tunis,  
Tunis el Manar University, El Manar, II 2092, Tunis, Tunisia  
0000-0002-8708-8548  
menallah.andolsi@fst.utm.tn

## Abstract

We explore the two-dimensional vector Duffin-Kemmer-Petiau (DKP) oscillator within the minimal length assumption. Using the momentum representation underlying the generalized uncertainty principle, we worked out exactly the corrected energy eigenvalues of the oscillator then we visualize some numerical solutions in the presence of the deformed algebra. In addition, the associated wave functions were expressed in terms of Jacobi polynomials. Moreover, we discussed the spin-1 boson dynamics in the presence of an external transverse homogeneous magnetic field.

## References

- [1] Y. Chargui, A. Dhahbi, Phys. Lett. A **457**, 128538 (2023).
- [2] Y. Chargui, A. Dhahbi, Eur. J. Phys. Plus **138**, 26 (2023).
- [3] Y. Chargui, A. Dhahbi, Eur. J. Phys. Plus **138**, 531 (2023).

# NEUMANN SIEVE PROBLEM REVISITED

Andrii **KHRABUSTOVSKYI**

Department of Physics, University of Hradec Králové  
Rokitanského 62, 500 03, Hradec Králové, Czech Republic  
0000-0001-6298-9684  
andrii.khrabustovskyi@uhk.cz

## Abstract

Let  $\Omega \subset \mathbb{R}^n$  be a domain, which is intersected by a hyperplane  $\Gamma$ . We make a lot of small holes  $D_{k,\varepsilon}$ ,  $k = 1, 2, 3, \dots$  in  $\Gamma \cap \Omega$ , where  $\varepsilon > 0$  is a small parameter; when  $\varepsilon \rightarrow 0$ , the number of holes tends to infinity, while their diameters tends to zero. Let  $\mathcal{A}_\varepsilon$  be the Neumann Laplacian in the perforated domain  $\Omega_\varepsilon = \Omega \setminus \Gamma_\varepsilon$ , where  $\Gamma_\varepsilon = \Gamma \setminus (\cup_k D_{k,\varepsilon})$  (“sieve”). It is well-known that under some critical scaling of the holes radii, the operator  $\mathcal{A}_\varepsilon$  converges in the strong resolvent sense to the Laplacian on  $\Omega \setminus \Gamma$  subject to the so-called  $\delta'$ -conditions on  $\Gamma \cap \Omega$ . In this talk we discuss some recent improvements of this result obtained in [A.K., Ann. Mat. Pura Appl. (2023), 202:1955–1990], where under rather general assumptions on the shapes and locations of the holes we derived estimates on the rate of convergence in terms of  $L^2 \rightarrow L^2$  and  $L^2 \rightarrow H^1$  operator norms.

## **THE KLEIN–GORDON OSCILLATOR IN THE PRESENCE OF A MINIMAL LENGTH**

**Asma MERAD**

Department of Physics, University of Batna1, Batna, Algeria  
asmamerad9@gmail.com

### **Abstract**

In this talk, We present an exact solution of the Klein–Gordon oscillator in the momentum space in the presence of minimal length uncertainty, The obtained results, namely the energy eigenvalues and eigenfunctions, present interesting characteristic behavior.



## CORRELATIONS IN 1D HOMOGENEOUS BOSE MIXTURES

Atika **MEHEDI**

Laboratory for Theoretical Physics and Material Physics, Department of Physics, Faculty of Exact Sciences and Informatics, Hassiba Benbouali University of Chlef, Algeria  
Ouled Fares, Chlef, 02000, Algeria  
0000-0003-4961-9536  
mahdimahdi053@gmail.com or a.mehedi@univ-chlef.dz

Fatima **KOUDJIL**

Laboratory for Theoretical Physics and Material Physics, Department of Physics, Faculty of Exact Sciences and Informatics, Hassiba Benbouali University of Chlef, Algeria  
Ouled Fares, Chlef, 02000, Algeria  
koudjilf95@gmail.com

Mohamed **BENAROUS**

Laboratory for Theoretical Physics and Material Physics, Department of Physics, Faculty of Exact Sciences and Informatics, Hassiba Benbouali University of Chlef, Algeria  
Ouled Fares, Chlef, 02000, Algeria  
m.benarous@univ-chlef.dz

### Abstract

Based on a semi classical approach, we have analyzed the equilibrium properties of binary mixture. By using a Gaussian density operator we derive the TDHFB equations from the Balian-Veneroni variational principle. The TDHFB equations are applied to a system of self-interacting trapped bosons to derive a coupled dynamics of the condensate, the non condensate and the anomalous densities. We determine variationally analytic expressions for both the anomalous and the non condensate densities for one, two and three dimensional systems. The anomalous averages and the non condensate densities for a 1D homogeneous bose mixture at zero temperature are computed numerically.

**Keywords:** Mean field Method, Semi-classical approach, Binary BEC, One-body correlations.

## THE FACT OF MOTION IN DIPOLAR BEC

Bakhta **CHERIFI**

LPTM, Faculty of Exact and Computer Sciences **Faculty**, Hassiba Benbouali University of Chlef  
Hassiba Benbouali university of Chlef , P.O.Box 78, 02000, Ouled-fares, Chlef, Algeria  
ba.cherifi@univ-chlef.dz

Abdelali **BOUDJEMAA**

LPTM, Faculty of Exact and Computer Sciences **Faculty**, Hassiba Benbouali University of Chlef  
Hassiba Benbouali university of Chlef , P.O.Box 78, 02000, Ouled-fares, Chlef, Algeria  
a.boudjmaa@univ-chlef.dz

### Abstract

We study the properties of a moving single dipolar BEC using the full Hartree-Fock-Bogoliubov theory. The analytical and numerical calculations emphasize that the interspecies dipole-dipole interactions may affect the behavior of the condensed depletion, The behavior of the LHY corrected-energy It is found that in the lower branch of the single, these quantities are unimportant and present an unconventional behavior.

### References

- [1] T. D. Lee, K. Huang and C. N. Yang, Phys. Rev **106**, 1135 (1957).
- [2] M. Wenzel, F. Bottcher, J-N. Schmidt, M. Eisenmann, T. Langen, T. Pfau, and I. Ferrier-Barbut, Phys. Rev. Lett. **121**, 030401 (2018).
- [3] A. Boudjemâa, J. Phys. B: At. Mol. Opt. Phys. **48**, 035302 (2015).
- [4] T. D. Lee, K. Huang and C. N. Yang, Phys. Rev **106**, 1135 (1957). Boudjemâa, J. Phys. B: At. Mol. Opt. Phys. **48**, 035302 (2015).

# AN ANALYSIS ON THE THERMAL QUANTITIES OF QUANTUM-CORRECTED SCHWARZSCHILD ADS BLACK HOLE SURROUNDED BY QUINTESSENCE MATTER

Bekir Can **LUTFUOGLU**

Department of Physics, University of Hradec Králové, Czechia  
0000-0001-6467-5005  
bekir.lutfuoglu@uhk.cz

Bilel **HAMIL**

Laboratoire de Physique Mathématique et Subatomique, Faculté des Sciences Exactes,  
Université Constantine 1, Constantine, Algeria. 0000-0002-7043-6104 hamilbilel@gmail.com

Laid **DAHBI**

Teacher Education College of Setif, Messaoud Zeghar, Algeria  
l.dahbi@ens-setif.dz

## Abstract

In this study, we explored the shadows and thermal quantities of a quantum-corrected Schwarzschild AdS black hole surrounded by quintessence matter. For this purpose, we attached the quintessence matter field terms to the lapse function of the quantum-corrected Schwarzschild AdS black hole. At first, we obtained the mass function, and we discussed the effects of the quintessence matter field in the presence and absence of quantum corrections. We observed that quantum corrections are effective only in relatively small event horizon radii. We found that the quintessence field effects are more effective on relatively greater event horizon radii. We also found that for a particular value of the quintessence state parameter, the black hole cannot exist for all event horizon values. Then, we derived the Hawking temperature. Our detailed analysis revealed similar effects of quantum corrections and quintessence matter fields. Then, we studied the entropy function. We showed that its functional form does not change. After that, we derived the Gibbs free energy and specific heat functions to discuss the stability of the black hole. We found that the black hole could be stable or unstable, depending on the event horizon value. Next, we found the geometric equation of state and investigated the isotherms graphically.

# CALCULATION OF PAIR CORRELATION FUNCTION IN GAS AND CRYSTAL PHASES OF TEMPERATURE SENSITIVE COLLOIDAL SYSTEM

Deniz **KAYA**

Physics Department, Science Faculty, Akdeniz University  
Antalya, TURKEY  
0000-0002-1951-2466  
denizkaya@akdeniz.edu.tr

## Abstract

Colloids are extensively used in technology and industry, while also playing a pivotal role in scientific endeavors. One notable example is their utilization in conjunction with light microscopes, which enables the association of micrometer-sized spherical colloid particles with atomic systems, constituting the fundamental building blocks of matter. This association serves as a valuable model system for investigating fundamental aspects of statistical mechanics, such as the mechanisms underlying phase transitions. The initial results of usage and calculation of pair interaction function in dilute and dense colloidal systems are shown in this study. We have used temperature sensitive microgel colloid particles to create a 2-dimensional (2d) gaseous phase (dilute) and 3-dimensional (3d) crystal (dense) phases. Images were taken under the light microscope and the positions of the particles were measured via image analysis techniques. From these data, pair correlation function were calculated for both systems which yielded the interaction potential between colloidal particles and various structural properties of the colloidal crystal were calculated.

## 1 Introduction

The structural characteristics of colloidal systems closely resemble those of atomic structures, and the precise measurement of colloid particle positions can be achieved with remarkable accuracy, thanks to the capabilities of light microscopy. Consequently, this enables the simultaneous execution of both local and dynamic measurements which cannot be achieved in atomic systems using existing technology. Such measurements involving colloid particles and light microscopy can yield novel insights into colloidal systems and shed light on previously unanswered questions within the realm of atomic systems. There are many studies who demonstrated this fact and readers can refer to the citations of an seminal paper by Crocker and Grier [1] for such applications. Through precise control of both the sensitivity and size of the synthesized colloid particles in response to temperature variations, we have been able to

simultaneously observe the interactions among these particles within confined geometries and under varying temperature conditions. This allowed us to measure their respective physical properties. In our study, we acquired the data through video microscope with the assistance of an image processing program. Subsequently, we directly computed the pair interaction potential energy of the colloid particles based on the particle positions of each particle in dilute and concentrated colloidal systems.

Our work is organized as follows: In the Materials and Methods section, we describe calculation of the pair correlation function in subsection 2.1 and the experimental details regarding synthesis of colloidal particles, preparing dilute (2d systems) and crystal (3d systems) in subsections of 2.2, 2.3, 2.4, respectively. Then the results of pair correlation function in dilute and crystal regimes are discussed in Results and Discussion section 3. Through our initial results in the study, the conclusions and the possible future studies and experiments are suggested in the section 4 .

## 2 Materials and Methods

### 2.1 Calculation of pair correlation function

The pair correlation function, denoted as  $g(r)$ , measures the distance between one particle and the central position of another particle, providing insight into the likelihood of finding particles at specific distances. In situations involving short distances, it characterizes the way particles arrange themselves, resembling the arrangement of closely packed hard spheres stacked atop each other. In such cases, the minimum possible separation between two particle centers corresponds to the diameter of the particles which is named as hard sphere system [2], [3]. Additionally,  $g(r)$  is normalized with respect to density, and for larger values, it converges towards a value of 1. For  $N(t)$  particles in the field of view at time  $t$ , distribution of particles can be expressed as

$$\rho(\mathbf{r}, t) = \sum_{j=1}^{N(t)} \delta(\mathbf{r} - \mathbf{r}_j(t)) \quad (1)$$

as  $j$  index scans through all individual particles as  $\mathbf{r}$  is the location of the particles [2]. For a system characterized by radially symmetric pairwise additive interactions, information can be extracted from two-body correlation function  $g(r)$ . Applying liquid structure theory, effective pair potential  $u(r)$  can be extracted from  $g(r)$  [4], [5], [6], [7]. From density pair distribution function  $g(\mathbf{r}_1, \mathbf{r}_2)$  for a homogeneous system can be written as follows:

$$g(\mathbf{r}_1, \mathbf{r}_2) = \left\langle \sum_{\alpha \neq \alpha'} \delta(\mathbf{r} - \mathbf{r}_\alpha(t)) \delta(\mathbf{r} - \mathbf{r}_{\alpha'}(t)) \right\rangle \quad (2)$$

By substituting Eq.1 into Eq.2, the pair correlation function can be expressed as

$$g(\mathbf{r}_1, \mathbf{r}_2) = \frac{1}{n^2} [\langle \rho(\mathbf{r}_1) \rho(\mathbf{r}_2) \rangle - \langle \rho(\mathbf{r}_1) \rangle \langle \rho(\mathbf{r}_2) \rangle] \quad (3)$$

where  $n = \langle \rho \rangle = N/A$  is the areal number density of particles. Given a particle at some location  $r_1$ ,  $g(r_1, r_2)$  is the probability of finding a second particle at location  $r_2$ . For transitionally invariant system, the pair distribution function is pair correlation function which can be interpreted as

$$g(\mathbf{r}) = \frac{1}{n} \left\langle \sum_{\alpha \neq 0} \rho(\mathbf{r} - \mathbf{r}_\alpha + \mathbf{r}_0) \right\rangle. \quad (4)$$

In this final form, the brackets represents averaging over time, angle and field of view. If the system is isotropic then radius can be expressed in terms of magnitude and hence  $g(r)$  becomes radial distribution function. Strong

correlation in a radial distribution function is expressed as the values higher than 1, in liquids the correlation increases with particle diameter and decreases adjacent to this region, at longer distances, correlation is 1. Radial distribution function is measured by counting pairs separated by  $r$  to  $r + dr$  and then normalized by  $2\pi r n dr$ .

The pair correlation function is related to potential of mean force,  $w(r)$  through Boltzman distribution;

$$w(r) \equiv -kT \ln[g(r)] \quad (5)$$

where  $w(r)$  reduces to  $u(r)$  at very low density limit. Since measurements are made in finite concentrations, many-body interactions may introduce additional structure into the pair correlation function. The resulting minima of  $w(r)$  is not the evidence of attraction, but describes many-body structural correlations. One should correct for the finite density by using approximation methods. Ornstein-Zernicke equation describes the evolution of many body interactions from a hierarchy of pairwise interactions [3]. Truncating the hierarchy results in approximations that may be inverted to obtain expressions for  $u(r)$ . Hypernetted Chain Approximation (HNC) is found to be accurate for soft potentials while Percus-Yevick (PY) is more accurate for short ranged interactions. The pair potential is evaluated with these formulas [8], [9], [10]: via Hypernetted chain approximation

$$u(r) = w(r) + kT n I(r) \quad (6)$$

and via Percus-Yevick approximation

$$u(r) = w(r) + kT n [1 + n I(r)]. \quad (7)$$

The term  $I(r)$  represents the iterative integration part, which is an convolution integral expressed as

$$I(r) = \int_A [g(r') - 1 - n I(r)] [g(|r' - r|) - 1] d^2 r'. \quad (8)$$

These equations can be solved iteratively to get the final interaction potential energy term expressed as  $u(r)$  [11].

## 2.2 Synthesis of colloidal particles

The synthesis of N-isopropylacrylamide (NIPAAm) microgels were performed by surfactant free emulsion polymerization method. In a 100 mL reaction flask, a mixture containing 0.5 g of N-isopropylacrylamide (NIPAAm), 0.016 g of acrylamide (AAm) monomers, 0.08 g of cross-linker methylenebisacrylamide (MBA), and 0.08 g of initiator (2,2-azobis (2-methylpropionamidine) hydrochloride (AMPDH)) dissolved in 50 mL of ultra-clean water was prepared. This solution was then placed in a water bath heated to 70 degrees Celsius, and polymerization was conducted under a nitrogen environment with continuous stirring at 70 degrees Celsius for a duration of 2 hours. Following the 2-hour polymerization period, the reaction flask was removed from the hot water bath and allowed to cool down to room temperature. After reaching room temperature, the resulting PNIPAAm particles were subjected to purification through centrifugation and subsequent washing with water on two occasions. The PNIPAAm colloidal particles were approximately 1 micron in size when measured by Mastersizer 2000 device.

## 2.3 Preperation of dilute systems

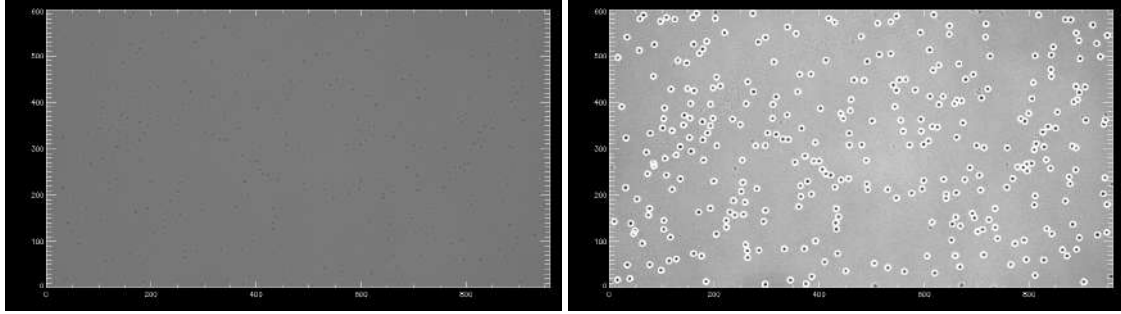
The 2d system was prepared by diluting the batch of synthesized PNIPAM colloidal particles by deionized water. The sample holder was two pieces of coverslips. The diluted solution was pipetted onto one of the cover slips so that the liquid formed a thin layer. Then the other coverslip was gently placed over this and the edges were sealed with epoxy for eliminating the evaporation. The sample thickness was less than two particle diameter thick so that particles could not diffuse in z direction. The temperature was set to room temperature ( $T = 23^\circ C$ ) by Warner Instrument stage and objective heater, where roughly 50000 images were taken.

## 2.4 Preparation of crystal systems

We used the same particles to create colloidal crystals with a similar experimental setup but in this case, the sample holder were the coverslips which separated by roughly  $100\text{ }\mu\text{m}$  thick of parafilm strips. The concentration of colloidal suspension was much more concentrated so that an amorphous or crystal phase could be achieved. The dense sample was pipetted into the channels of the sample holder. After closing the gaps with epoxy, the sample was placed onto the light microscope. The initial phase of the system was amorphous and the temperature was raised to melt the sample. The melt was cooled down gradually to grow crystals, heating-cooling annealing steps were repeated until a crystal grain was grown. For the crystal grain, we acquired 10000 images at five different temperatures. For all images, the image analysis routines were performed to get subpixel resolution [1].

## 3 Results and Discussion

Following the procedure described in the previous sections, first we identified the particle via image analysis techniques. In figure 3 the raw image is shown, the particles are identified in figure 3. Following the steps of calculation in section 2.1,  $g(r)$  and  $u(r)$  was calculated.



(a) Contrast enhanced image of a colloidal particles in 2d system      (b) Particle locations laid over the image

Figure 1: Steps of image analysis

For the 2d dilute system, a peak has been observed at  $r = 0.94\text{mm}$  for in both Fig. 3 and Fig.3. For  $g(r)$ , this means the correlation value is the highest at that distance, hence the highest probability of finding a particle shown in Fig. 3. The interaction potential  $u(r)$  reveals the min value around that location which can be interpreted as attraction force shown in Fig.3. Since the magnitude of the negative potential was about  $-0.3k_B T$ , the particles do not got stuck to each other at room temperature. Other result from the interaction potential is the repulsion part as in hard sphere model of interaction potential which was an expected property of colloidal systems.

The crossectional view of 3d crystal grain is shown in Fig. 3 where the boundaries are emphasized with red lines. The crystal grain was around  $90 \times 60\text{ }\mu\text{m}$  in size and the layer of crystal studied in this work was located roughly  $30\text{ }\mu\text{m}$  above the bottom coverslip. After finding the particle locations with subpixel resolution, pair correlation function (radial distribution function) was calculated for each temperature. These  $g(r)$  functions were rescaled on their maximum value, which corresponds to their first peak as shown in Fig.3. In concentrated colloidal crystals, the crossectional layers were [111] plane of FCC (Face centered cubic) crystal. The peaks of  $g(r)$  correspond to the correlation of finding the neighbors of the central particle, starting from the nearest one which is the first and the highest peak. With increasing temperature, the particles were fluctuating more which yielded wider distributions in

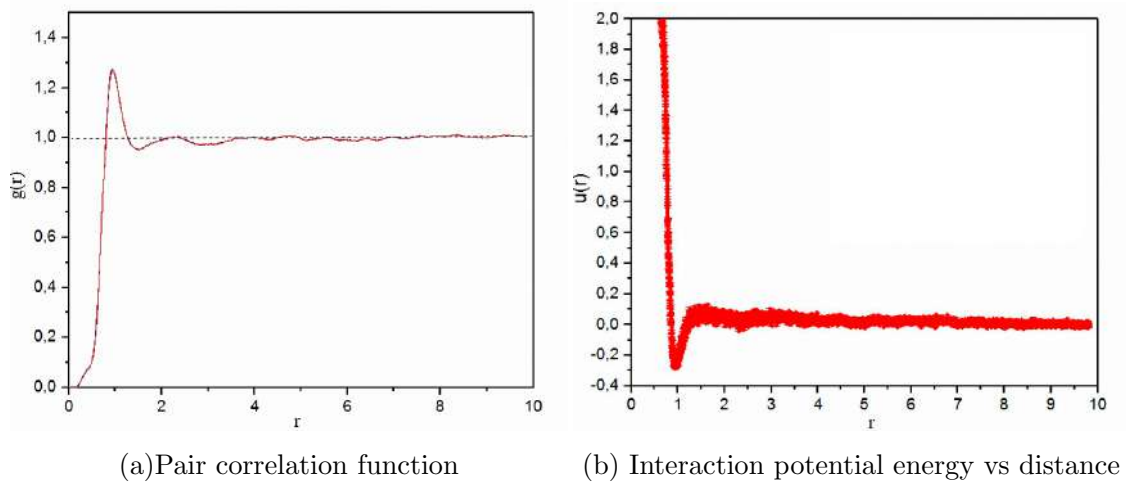


Figure 2: Results of 2d dilute system

$g(r)$  distributions. Since the graph in Fig. 3 is normalized according to the first peak, the change in the distributions of the second and third peaks can be studied in detail.

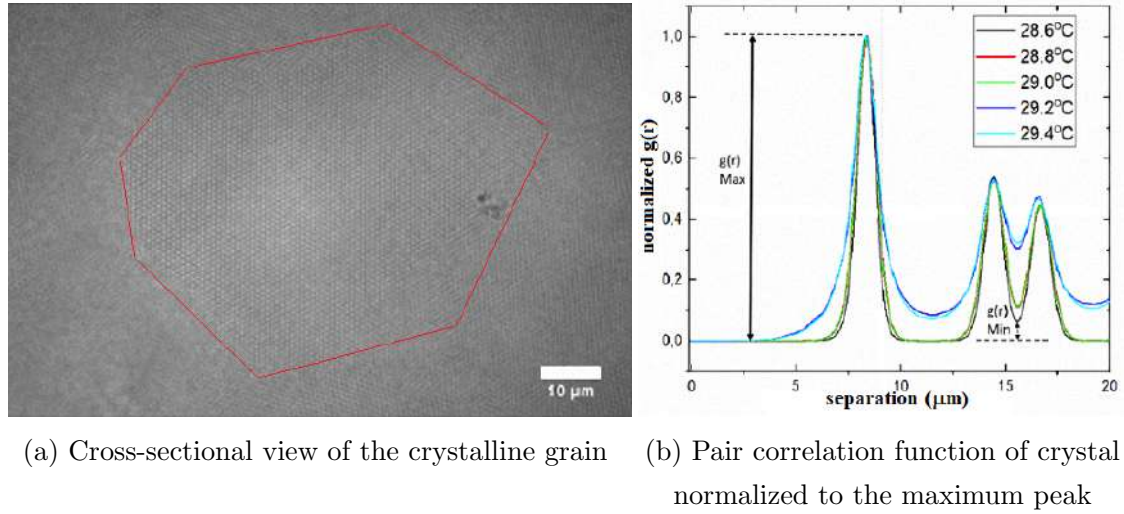


Figure 3: Crystalline grain and the corresponding pair correlation function at various temperatures

The detailed analysis of  $g(r)$  in the crystal data were shown in Fig.4. The first peak was fitted to a Gaussian function and the width was calculated. The width is increasing with the temperature as shown in Fig.3. Also, the ratio of the maximum value (which is normalized to value of 1 for all peaks) and the minimum value of  $g(r)$  was shown in Fig3. This ratio is decreasing as the temperatures increases. These results show the phase of the crystal as



it is been heated towards melting. Both graphs show two different regions as the rate of change in  $g(r)$  have changed around 28.8 °C. We should emphasize the fact that, at the highest temperature, the crystal did not melt. Further analysis such as dynamics of individual particles, and location of each particle with respect to the grain boundary can be done to understand this behavior better [12]. Since the melting had not happened at the temperatures studied in the system, analysis of  $g(r)$  function reveals two region within the melt phase.

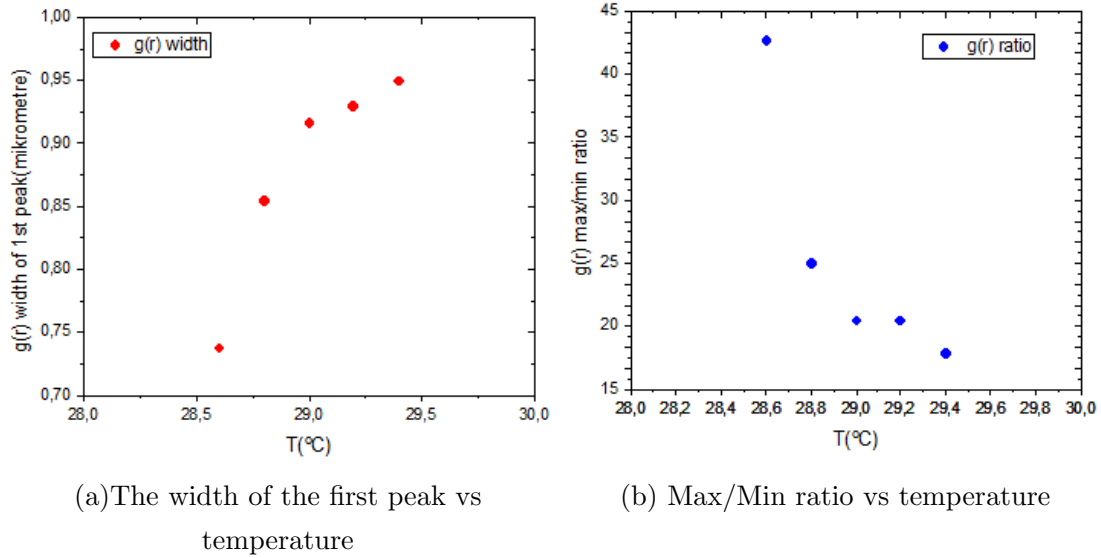


Figure 4: Analysis of the  $g(r)$  function at various temperatures

## 4 Conclusion

We have shown the steps of calculation pair correlation function for colloidal systems of two different phases. In the dilute phase, the resultant interaction potential energy showed a  $-0.3 k_B T$  value which might be a indication of attraction between the particles at room temperature. In order to make a conclusion of such, we need to take care of imaging artifact due to closely located particles. Also in order to understand how interaction potential changes with temperature, data should be taken at different temperatures which we plan to do in near future. For the 3d system of colloidal crystal, analysis of  $g(r)$  pair correlation function yielded an evolution at different temperatures. The distribution and height of each peak reveals the changes between the particle distances as the system was heated towards melting temperature. Since the sample studied was not a bulk crystal but a crystal grain, the boundary effects played a crucial role in the results. Similar analysis must be repeated to understand the effect of the size for much bigger crystals to identify the dynamics of melting in our temperature sensitive colloidal crystal system.

## Acknowledgements

*This work have been supported by TUBITAK grant number 116M396.*

## References

- [1] J.C. Crocker, and D.G. Grier, Colloid and Inter. Sci. **179**, 298, (1996).
- [2] P. M. Chaikin and T. C. Lubensky, Principles of Condensed Matter Physics, Cambridge University Press, Cambridge, (1995).
- [3] D. A. McQuarrie, Statistical Mechanics, University Science Books, Mill Valley, CA, (2000).
- [4] G. M. Kepler and S. Fraden Phys. Rev. Lett. **73**, 356 (1994).
- [5] J.C. Crocker, and D.G. Grier, Phys. Rev. Lett. **73**, 352 (1994).
- [6] K. Vondermassen, J. Bongers, A. Mueller and H Versmold. Phys. Rev. Lett **10**, 1351 (1994).
- [7] M. Mungan, C.-H. Sow, S. N. Coppersmith, and D. G. Grier, Phys. Rev. B **58**, 14588 (1998).
- [8] M. D. Carbajal-Tinoco, F. Castro-Román, and J. L. Arauz-Lara, Phys. Rev. E **53**, 3745 (1996).
- [9] S. H. Behrens and D. G. Grier, Phys. Rev. E **64**, 050401 (2001).
- [10] E. M. Chan, J. Phys. C **10**, 3477 (1977).
- [11] Y. Han and D.G. Grier, Phys. Rev. Lett. **91**, 038302 (2003)
- [12] A.M. Alsayed, M.F. Islam, J.Zhang, P.J. Collings and A.G. Yodh, Science **309**, 1207 (2005)

# RADIUS OF THE WHITE DWARF ACCORDING TO FERMI ENERGY IN A $\kappa$ -DEFORMED FRAMEWORK

Fariba **KAFIKANG**

Faculty of Physics, Shahrood University of Technology  
P. O. Box : 3619995161-316., Shahrood, Iran  
0000-0001-7110-3830  
f.kafi19@yahoo.com

Hassan **HASSANABADI**

Faculty of Physics, Shahrood University of Technology  
P. O. Box : 3619995161-316., Shahrood, Iran  
0000-0001-7487-6898 (hha1349@gmail.com)

Won-Song **CHUNG**

Department of Physics and Research Institute of Natural Science,  
College of Natural Science,  
Gyeongsang National University, Jinju 660-701, City, Korea.  
mimip44@naver.com

## Abstract

In this article, the  $\kappa$ -deformation formalism, which is in the form of  $e_k(x) = (\sqrt{1 + \kappa^2 x^2} + \kappa x)^{(\frac{1}{\kappa})}$ , is investigated. Using the  $\kappa$ -deformation, the Fermi energy, for box problem with the Schrödinger equation, has been investigated and calculated. In addition, we calculated the internal energy and pressure, and also calculated the radius of the white dwarf with the pressure due to degeneracy and gravity.

# BOSE GAS OF A QUASI TWO-DIMENSIONAL HARMONICALLY TRAPPED IN THE DUNKL ALGEBRA

Fateh **MERABTINE**

Laboratory for Theoretical Physics and Material Physics Faculty of Exact Sciences and Informatics, Hassiba Benbouali University of Chlef.  
Oulad Fares, Chlef, 02000, Algeria  
merabtinefateh172@gmail.com

Bilel **HAMIL**

Laboratoire de Physique Mathématique et Subatomique, Faculté des Sciences Exactes,  
Université Constantine 1, Constantine, Algeria. 0000-0002-7043-6104 hamilbilel@gmail.com

Ahmed **HOCINE**

Laboratory for Theoretical Physics and Material Physics Faculty of Exact Sciences and Informatics, Hassiba Benbouali University of Chlef.  
Oulad Fares, Chlef, 02000, Algeria  
hoahmed72@yahoo.fr

## Abstract

In the context of Dunkl-Boson theory, our work focuses on exploring the Bose-Einstein condensation of Dunkl-Bosons. This system is characterized by a finite number of particles and is trapped in a two dimensional harmonic potential trap. We employ a modified density of states method to analyze this phenomenon, we obtain the expressions of the effective Dunkl-critical temperature  $T_c^D$ , the ground state population  $N/N_0^D$ , the Dunkl-internal energy  $U^D$  and the Dunkl-specific heat function  $C^D$ . The numerical calculations show that the Dunkl-Bose-Einstein condensation in this system exhibits particular and intriguing characteristics distinct from those observed in a conventional trapped boson system. We think that this work has the potential to offer significant insights into the Dunkl-deformed boson theory and could be valuable for future exploration of Bose-Einstein condensation involving trapped Dunkl-Bosons

## References

- [1] F. Merabtine, B. Hamil, B. C. Lutfuoglu, A. Hocine, M. Benarous, J. Stat. Mech. **5**, 053102 (2023).

- [2] A. S. Hassan, A.M. El-Badry, Physica B **404**, 1947 (2009).
- [3] Q. -J. Zeng, Y. -S. Luo, Y. -G. Xu, H. Luo, Physica A **398**, 116 (2014).
- [4] A. Hocine, B. Hamil, F. Merabtine, B. C. Lutfuoglu, M. Benarous, arXiv:2308.10891.
- [5] B. Hamil, B. C. Lutfuoglu, Physica A **623**, 128841 (2023).

## TRIPLE BOSE MIXTURES ON A SINGLE SPECIES

Fatima **KOUDJIL**

Laboratory for Theoretical Physics and Material Physics LPTPM QUANTUM GASES GROUP, Department of  
Physics Faculty of Exact Sciences and Informatics Hassiba Ben Bouali University- Chlef  
Zeboudja, 2014, Chlef, Algeria  
fa.koudjil@univ-chlef.dz

Atika **MEHEDI**

Laboratory for Theoretical Physics and Material Physics, Department of Physics, Faculty of Exact Sciences and  
Informatics, Hassiba Benbouali University of Chlef (Algeria)  
Ouled Fares, Chlef, 02000, Algeria  
0000-0003-4961-9536  
a.mehedi@univ-chlef.dz

Mohamed **BENAROUS**

Laboratory for Theoretical Physics and Material Physics LPTPM QUANTUM GASES GROUP , Department of  
Physics Faculty of Exact Sciences and Informatics Hassiba Ben Bouali University- Chlef  
chlef, 2400, Chlef, Algeria  
m.benarous@univ-chlef.dz

### Abstract

In this work, we will study the trimer correlations of triplets states in a single-species Bose gas system, This is performed by a consistent variational approach, free of perturbative hypothesis by examining whether these results accurately describe the physics by calculating certain physical parameters.

### References

- [1] H Flocard, Variational Extension of the Time-Dependent Mean-Field Approach, Ann. of Phys. (N.Y.) 191 (1989), 382.
- [2] M. Benarous, Extensions variationnelles de la méthode du champ moyen dépendant du temps. PhD thesis, IPN-ORSAY-France, 1991.
- [3] B. Cherifi, Effet du triplet dans un gaz piégé ultra-froids, Magister Thesis, USTHB Algiers, Algeria, 2013.

**PHYSICS EDUCATION and RESEARCH IN I. U.****Y. Gürkan ÇELEBİ**

Department of Physics, Istanbul University, Istanbul Turkey  
gcelebi@istanbul.edu.tr

**Abstract**

It seems we have a problem and I don't exactly know how to address it. Current state of physics and education here in I.U. is in trouble. Over more than 30 years, I have been observing the decay in our education system in our department. Even the most fundamental concepts of physics is foreign to our graduates not to mention the scientific process that they should have been equipped for during their education. Yet, the number of publications that coming out of our department per year has been increasing at an accelerated rate in parallel to the number of faculty member that we are accumulating by promoting from our current researchers and teaching assistants. I would like to talk about these seemingly contradictory trends and discuss the possible reasons why this is becoming our current state of education and research.

# NON-COMMUTATIVE KLEIN-GORDON EQUATION AND MECHANISM OF SCALAR PARTICLES PAIR PRODUCTION

Hadjar **REZKI**

Department of Physics, Faculty of Material Sciences, University of Batna 1  
Street 19 mai, Road of Biskra - Batna, 05 000 Algeria  
0009-0003-9687-1723  
hadjar.rezki@univ-batna.dz

Slimane **ZAIM**

Department of Physics, Faculty of Material Sciences, University of Batna 1  
Street 19 mai, Road of Biskra - Batna, 05 000 Algeria  
slimane.zaiem@univ-batna.dz

## Abstract

The phenomena of scalar particles being created in a non-commutative space-time setting in the presence of an electric field is investigated here. Our goal is to investigate the role that the electric field plays in the emergence of particles from the vacuum of space. We have determined the number density of spin-0 produced particles in a non-commutative space-time by using the Bogoliubov transformation approach. We explored the process of particle creation from solutions that are expressed in terms of special functions. Our research was conducted in accordance with the formalism of the Klein-Gordon equation in non-commutative space-time. The findings have been analyzed and evaluated. The results obtained from this study provide confirmation of the phenomenon of particle production as a characteristic of curved space-time. Moving forward, our objective is to investigate the process of Dirac particle generation inside non-commutative spaces.

## References

- [1] J. Garriga, Phys. Rev. D **49**, 6343 (1994).
- [2] S. Haouat and R. Chekireb, Eur. Phys. J. C **72**, 2034 (2012).
- [3] S. Zaim and L. Khodja, Phys. Scr. **81**, 055103 (2010).
- [4] I.S.Gradshteyn, I. M. Ryzhik, Table of Integrals, Series and Products.



## MICROANALYSES OF 3D-PRINTED PRODUCTS MADE OF THERMOPLASTICS BY THE HOT-MELT EXTRUSION METHOD

Jan LOSKOT

Department of Physics, University of Hradec Králové  
Rokitanského 62, 500 03, Hradec Králové, Czech Republic  
0000-0003-0172-4353  
jan.loskot@uhk.cz

### Abstract

This contribution provides a general overview of extrusion-based 3D printing from thermoplastic materials, its applications, and methods of analysis of the printed products on a microscopic scale. We focused on assessing the influence of print speed on the characteristics of products made from glycol-modified polyethylene terephthalate (PETG) by fused filament fabrication (FFF) technology. The study involves a comprehensive analysis of the microstructure and morphology of the printed PETG products using scanning electron microscopy (SEM), surface roughness testing, and X-ray microtomography (microCT) imaging. Notably, higher print speeds were found to result in the formation of structural anomalies and voids, affecting both the surface and internal features of the printed items. Additionally, a non-linear relationship between print speed and the orientation of polymer chains in the printed material was found by means of polarized Raman spectroscopy. This alignment of PETG chains is unlikely to be the primary cause of the surface voids, but there are some potential correlations of the chain alignment degree with some micromechanical properties (Vickers microhardness, Young's modulus, indentation work) of the printed material. The research concludes that print speeds up to  $60 \text{ mm s}^{-1}$  are suitable for printing PETG with our printer configuration. Overall, this contribution offers comprehensive insights into analyzing products made by hot melt extrusion of polymeric materials, thus showing ways to improve the output quality control of the products.

# QUANTUM LIQUID DROPLETS IN BOSE MIXTURES WITH WEAK DISORDER

Karima **ABBAS**

Department of physics, Faculty of Exact Sciences and Informatics, and Laboratory of Mechanics and Energy,  
Hassiba Benbouali University of Chlef  
P.O. Box 78, 02000, Ouled-Fares, Chlef, Algeria  
k.abbas@univ-chlef.dz

Abdelaali **BOUDJEMAA**

Department of physics, Faculty of Exact Sciences and Informatics, and Laboratory of Mechanics and Energy,  
Hassiba Benbouali University of Chlef  
P.O. Box 78, 02000, Ouled-Fares, Chlef, Algeria  
a.boudjemaa@univ-chlef.dz

## Abstract

We study the properties of self-bound liquid droplets of three-dimensional Bose mixtures in a weak random potential with Gaussian correlation function at both zero and finite temperatures. Using the Bogoliubov theory, we derive useful formulas for the ground-state energy, the equilibrium density, the depletion, and the anomalous density of the droplet. The quantum fluctuation induced by the disorder known as the glassy fraction is also systematically computed. At finite temperatures, we calculate the free energy, the thermal equilibrium density, and the critical temperature in terms of the disorder parameters. We show that when the strength and the correlation length of the disorder potential exceed a certain critical value, the droplet evaporates and is eventually entirely destroyed. We calculate the density profiles of this exotic state by means of numerical simulations of the corresponding generalized disorder Gross-Pitaevskii equation. Our predictions reveal that as the strength of the disorder gets larger, the atomic density varies rapidly in the plateau region. We point out in addition that the peculiar interplay of the disorder and the repulsive Lee-Huang-Yang corrections play a pivotal role in the collective modes of the self-bound droplet.

## References

- [1] D. S. Petrov, Phys. Rev. Lett. **115**, 155302 (2015).

- [2] C. R. Cabrera, L. Tanzi, J. Sanz, B. Naylor, P. Thomas, P. Cheiney, L. Tarruell, *Science* **359**, 301 (2018).
- [3] A. Boudjemâa and K. Abbas, *Phys. Rev. A* **102**, 023325 (2020).
- [4] A. Boudjemâa, *Phys. Rev. A* **98**, 033612 (2018).
- [5] L. Sanchez-Palencia, D. Clément, P. Lugan, P. Bouyer, and A. Aspect, *New J. Phys.* **10**, 045019 (2008).

## MICROSTRUCTURE CHARACTERISTIC OF $(\text{TiTaNbZr})_{100-x}\text{Cu}_x$ HIGH ENTROPY ALLOYS FOR POTENTIAL ANTIBACTERIAL PROPERTIES

Karsten **GLOWKA**<sup>1</sup>, Agata **KASPERCZYK**<sup>1</sup>, Maciej **ZUBKO**<sup>1,2</sup>, Krystian **PRUSIK**<sup>1</sup>, Grzegorz **DERCZ**<sup>1</sup>, Paweł **ŚWIECK**<sup>1</sup> and Danuta **STRÓŻ**<sup>1</sup>

<sup>1</sup>Institute of Materials Engineering, University of Silesia in Katowice,  
75 Pułku Piechoty 1a, 41-500 Chorzów, Poland.

<sup>2</sup>Department of Physics, University of Hradec Králové,  
Rokitanského 62, 500 03, Hradec Králové, Czech Republic.  
karsten.glowka@us.edu.pl

### Abstract

Multi-principal elements alloys (MPEAs) have drawn large attention of the scientific community around the globe. The novel and innovative group of MPEAs includes high entropy alloys (HEAs). The first published independent studies about HEAs were literature-reported in 2004 [1,2]. In this year, two definitions of high entropy materials based on the chemical composition and mixing entropy ( $\Delta S_{mix}$ ) have been proposed [3]. HEAs are being more widely used in various applications due to their promising properties for example in biomedicine. Materials for biomedical applications belong to a particular group of engineering materials. The chemical composition must include mostly biocompatible elements [4]. The literature data revealed that biomedical high entropy alloys (bio-HEAs) exhibit high biocompatibility, improved mechanical properties, and higher corrosion resistance in comparison to conventional alloys [5–7]. It was also presented that the antibacterial properties of bio-HEAs could be denoted as new future trends in biomedical high entropy materials [8]. Literature data showed that copper (Cu) could be classified as an antibacterial element. It was reported that Cu-ions favour the inactivation process of bacteria [8]. Moreover, antibacterial alloys could be very beneficial in the current medical applications. In the presented studies the influence of Cu-addition on the structure and properties of  $(\text{TiTaNbZr})_{100-x}\text{Cu}_x$  (where:  $x = 0, 5, 7, 10, 15, 20$  at. entropy alloys) was investigated. Samples were obtained from elemental powders followed by blending in a high-energy ball mill to improve homogeneity. As-blended powders were pressed and further melted using the vacuum arc-melting technique. Obtained buttons were heat-treated and followed by a rapid quench in ice water. In the presented work results of the X-ray diffraction

(XRD) phase analysis, transmission electron microscopy (TEM) microstructure analysis, scanning electron microscopy (SEM), Energy Dispersive Spectroscopy (EDS) and mechanical properties analysis will be discussed.

**Keywords:** high entropy alloys, microstructure, antibacterial properties

## References

- [1] B. Cantor, I.T.H. Chang, P. Knight, A.J.B. Vincent, Microstructural development in equiatomic multicomponent alloys, *Mater. Sci. Eng. A*. **375–377**, 213–218 (2004). doi:<https://doi.org/10.1016/j.msea.2003.10.257>.
- [2] J.-W. Yeh, S.-K. Chen, S.-J. Lin, J.-Y. Gan, T.-S. Chin, T.-T. Shun, C.-H. Tsau, S.-Y. Chang, Nanostructured High-Entropy Alloys with Multiple Principal Elements: Novel Alloy Design Concepts and Outcomes, *Adv. Eng. Mater.* **6**, 299–303 (2004). doi:<https://doi.org/10.1002/adem.200300567>.
- [3] Y. Zhang, History of High-Entropy Materials, in: *High-Entropy Mater. A Br. Introd.*, Springer Singapore, Singapore, 2019: pp. 1–33. doi:10.1007/978-981-13-8526-1-1
- [4] A. Biesiekierski, J. Wang, M. Abdel-Hady Gepreel, C. Wen, A new look at biomedical Ti-based shape memory alloys, *Acta Biomater.* **8** (2012) 1661–1669. doi:10.1016/j.actbio.2012.01.018.
- [5] N. Hua, W. Wang, Q. Wang, Y. Ye, S. Lin, L. Zhang, Q. Guo, J. Brechtel, P.K. Liaw, Mechanical, corrosion, and wear properties of biomedical Ti–Zr–Nb–Ta–Mo high entropy alloys, *J. Alloys Compd.* **861**, 157997 (2021). doi:10.1016/j.jallcom.2020.157997.
- [6] S.P. Wang, J. Xu, TiZrNbTaMo high-entropy alloy designed for orthopedic implants: As-cast microstructure and mechanical properties, *Mater. Sci. Eng. C*. **73**, 80–89 (2017). doi:10.1016/j.msec.2016.12.057.
- [7] T. Hori, T. Nagase, M. Todai, A. Matsugaki, T. Nakano, Development of non- equiatomic Ti-Nb-Ta-Zr-Mo high-entropy alloys for metallic biomaterials, *Scr. Mater.* **172**, 83–87 (2019). doi:10.1016/j.scriptamat.2019.07.011.
- [8] E. Zhang, X. Zhao, J. Hu, R. Wang, S. Fu, G. Qin, Antibacterial metals and alloys for potential biomedical implants, *Bioact. Mater.* **6**, 2569–2612 (2021). doi:10.1016/j.bioactmat.2021.01.030.

## LOW-COST COPPER THIOCYANATE AS AN ALTERNATE HOLE-TRANSPORT MATERIAL FOR PEROVSKITE SOLAR CELLS

Devarepally Kishore **KUMAR**

Blaustein Institutes for Energy Research, Ben-Gurion University of the Negev, Israel

0000-0003-0125-1517

nanokishore@gmail.com

### Abstract

For photo-generated charge transport, choice of interfacial layers are important are important for improving the performance of perovskite solar cells (PSCs). In n-i-p architecture of PSCs, spiro-OMeTAD has been widely used as hole transport material (HTM). However, the same is costly and processing of its thin film is complex. Moreover, due to its low mechanical toughness cracks are induced in the film which results in penetration of moisture and oxygen in the perovskite layer. Copper thiocyanate (CuSCN) has been a good alternative to spiro-OMeTAD and has resulted in comparable power conversion efficiency (PCE). It possesses high hole mobility, wide bandgap, chemical and thermal stability and solution processability that makes it a good choice for HTM of perovskite solar cells. In this work, the role of CuSCN as HTM in triple cation perovskite solar cells in the stability studies is discussed. Triple cation perovskite cells with CuSCN HTM are tested for indoor and outdoor photostability studies under one Sun condition and the average T 80 of the devices exceeded when compared to perovskite cells with Spiro as HTL.

# DUFFIN KEMMER PETIAU OSCILLATOR IN A UNIFORM MAGNETIC FIELD IN ANTI de SITTER SPACE

Lakhdar **SEK**

Department of Technology, Faculty of Technology, Eloued University  
0009-0004-0582-5949  
sek-lakhdar@univ-eloued.dz

Mokhtar **FALEK**

Department Physics, Faculty of Sciences, University of Khenchela  
BP 1252 Road of Batna, 40004, Khenchela, Algeria  
0000-0002-0466-9559  
falekmokhtar75@gmail.com

Mustafa **MOUMNI**

LabPRIM, Faculty of Matter Sciences, University of Batna1  
Allees 19 mai, Route de Biskra, 05000, Batna, Algeria  
0000-0002-8096-6280  
m.moumni@univ-batna.dz

## Abstract

The study of the two dimensional bosonic oscillator equation within a uniform magnetic field was investigated analytically. We consider the presence of a minimal uncertainty in momentum caused by anti de Sitter space. Hence, the energy eigenvalues and the wave functions are obtained using Nikiforov Uvarov method and we deduced that the study leads to the same system of Klein Gordon (spin0). For spin 1 dkp case, we deduce the behaviour of the DKP equation and write the non relativistic energies and we show that the space deformation adds a new spin orbit term.

**Keywords:** DKP equation, Anti deSitter space, scalar and vector cases.

# STATISTICAL DESCRIPTIONS OF IDEA GAS FROM POSITION DEFORMED NONCOMMUTATIVITY

Latévi M. **LAWSON**

African Institute for Mathematical Sciences (AIMS) Ghana  
P.O. Box LG DTD 20046, Legon, Accra, Ghana  
latevi@aims.edu.gh

## Abstract

A set of position-dependent noncommutative algebra in two dimension (2D) that describes the space near the Planck scale had been introduced [1]. This algebra predicted the existence of minimal and maximal length uncertainties from position-dependent noncommutativity and a minimal momentum arising from generalized versions of Heisenberg's uncertainty relations. It is well known from Kempf *et al* formalism [2] that, the presence of minimal uncertainties raise the question of singularity of the space i.e the space is inevitably bounded by minimal quantities beyond which any further localization of particle is not possible. In the present paper, to avoid the difficulties in dealing with the minimal uncertainties which restrict the dimension of the wave function representations, we reduce this algebra through first order approximations of deformed parameters  $\tau, \theta$ . These approximations lead to a new position-dependent noncommutativity. In this new noncommutative space, we analytically solve the Schrödinger-like equation which describes a free particle system in a null quantum well potential. The spectrum of this system is asymmetrically deformed and exhibits different behaviours from the one obtained in ordinary quantum mechanics. Thus, we observe that by increasing the reduced deformed parameter  $\tau_r$ , the energy decreases and this decrease is more pronounced as the quantum number increases. Finally, we evaluate the thermodynamic quantities within the canonical ensemble and we show that these results are consistent with the ones recently obtained by Bensalem and Bouaziz [3].

**Keywords:** Noncommutative quantum mechanics; Position-dependent mass systems, Partition function of ideal gas.

## References

- [1] L. Lawson, J. Phys. A: Math. Theor. 53, 115303 (2020)
- [2] A. Kempf, G. Mangano and R. Mann, Phys. Rev. D **52**, 1108 (1995)



- [3] Bensalem and Bouaziz, Phys A. Stat. Mech. Its Appl. 523, 583-592 (2019)

# THE WEYL EQUATION IN THE SOM-RAYCHAUDHURI SPACE-TIME IN THE PRESENCE OF AN EXTERNAL ELECTROMAGNETIC FIELD

Mahsaalsadat **HOSSEINI**

Physics Department, Shahrood University of Technology  
Haft Tir Street, 3619995161-316, Shahrood, Iran  
0000-0001-6333-6650  
mahsahosseini16.mh@gmail.com

Hassan **HASSANABADI**

Physics Department, Shahrood University of Technology  
Haft Tir Street, 3619995161-316, Shahrood, Iran  
0000-0001-7487-6898  
hha1349@gmail.com

Somayyeh **HASSANABADI**

Department of Physics, University of Hradec Králové  
Rokitanského 62, 500 03, Hradec Králové, Czechia  
0000-0003-3928-3549  
s.hassanabadi@yahoo.com

## Abstract

In this presentation, we consider a massless spinor Dirac particle in the background gravitational field of the Som-Raychaudhuri space-time in order to study the influence of topology on this system. It is shown that the presence of the topological defect breaks the degeneracy of energy levels depending on the angular deficit which does not occur in usual space-time. We describe the Som-Raychaudhuri space-time by considering an external electromagnetic field. We obtain solutions of the Weyl equation by the Quasi-exact solvability (QES) method. We also obtain the eigenfunctions and the energy levels of the relativistic field.

## References

- [1] K. Gödel, Rev. Mod. Phys. **21**, 447 (1949).
- [2] F. Lobo and P. Crawford, NATO Sci.Ser.II **95**, 289 (2003).
- [3] S. Hawking, Phys. Rev. D **46**, 603 (1992).

- 
- [4] B. D. B. Figueiredo, I. D. Soares, and J. Tiomno, *Class. Quantum Grav.* **9**, 1593 (1992).
  - [5] N. Drukker, B. Fiol, and J. Simón, *JCAP* **0410**, 012 (2004).
  - [6] S. Das and J. Gegenberg, *Gen. Rel. Grav.* **40**, 2115 (2008).
  - [7] V. M. Villalba and C. de Física, *Mod. Phys. Lett. A* **8**, 3011 (1993).
  - [8] A. Vilenkin, *Phys. Rep.* **121**, 263 (1985).
  - [9] M. Barriola and A. Vilenkin, *Phys. Rev. Lett.* **63**, 341 (1989).
  - [10] J. Carvalho, A. M. de M. Carvalho, and C. Furtado, *Eur. Phys. J. C* **74**, 2935 (2014).
  - [11] G. Q. Garcia, J. R. de S. Oliveira, K. Bakke, and C. Furtado, *Eur. Phys. J. Plus* **132**, 123 (2017).
  - [12] L. C. N. Santos and C. C. Barros Jr, *Eur. Phys. J. C* **77** 186 (2017).
  - [13] J. P. Morais Graca, *Class. Quantum Grav.* **33**, 055004 (2016).
  - [14] A. F. Ratiada, *J Phys A Math Gen* **11** 341 (1978).
  - [15] R. Finkelstein, C. Fronsdal, and P. Kaus, *Phys. Rev.* **103** 1571 (1956).
  - [16] G. Q. Garcia, J. R. de S. Oliveira, and C. Furtado, *arXiv:1705.10631 [hep-th]*, (2017).
  - [17] S. Hassanabadi, J. Kríž, B. C. Lütfüoğlu, and H. Hassanabadi, *Physica Scripta* **97** 12 (2022).

# MAGNETIC QUANTUM GRAPHS WITH TIME-REVERSAL NON-INVARIANT VERTEX COUPLING

Marzieh **BARADARAN**

Department of Physics, Faculty of Science, University of Hradec Králové  
Rokitanského 62, 500 03 Hradec Králové, Czechia,  
0000-0002-8455-9973  
marzie.baradaran@yahoo.com

## Abstract

Motivated by the application of quantum graphs to model the anomalous Hall effect, we discuss spectral properties of periodic quantum graphs assuming that the vertex coupling is non-invariant with respect to the time reversal. Special attention is paid to the asymptotic behavior of the spectral bands in the high-energy regime; we see that the Band-Berkolaiko universality holds as long as the graph edge lengths are incommensurate. Moreover, we see that the transport properties of the graphs depend on the network topology, in particular, on the parity of the vertices involved.

This is a joint work with Pavel Exner and Jiří Lipovský based on Refs. [1] and [2].

## References

- [1] M. Baradaran, P. Exner, and J. Lipovsky, J. Phys. A: Math. Theor. **55**, 375203 (2022).
- [2] M. Baradaran, P. Exner, and J. Lipovsky, Ann. Phys. **454**, 169339 (2023).

## APPROXIMATE SOLUTIONS OF THE ROSEN-MORSE POTENTIAL BY MEANS OF THE NIKIFOROV-UVAROV METHOD

Meriem **ABDELAZIZ**

LabPRIM, Faculty of Matter Sciences, University of Batna1  
Allees 19 mai, Route de Biskra, 05000, Batna, Algeria  
meriem.abdelaziz@univ-biskra.dz

Mustafa **MOUMNI**

LabPRIM, Faculty of Matter Sciences, University of Batna1  
Allees 19 mai, Route de Biskra, 05000, Batna, Algeria  
0000-0002-8096-6280  
m.moumni@univ-batna.dz

Mokhtar **FALEK**

Department Physics, Faculty of Sciences, University of Khenchela  
BP 1252 Road of Batna, 40004, Khenchela, Algeria  
0000-0002-0466-9559  
falekmokhtar75@gmail.com

### Abstract

The use of approximated methods to solve the Schrödinger equation plays a vital role in exploring various aspects of diatomic molecules (DMs) such as their spectroscopic properties, electronic structure, and energetic characteristics. In this study, we employed the Nikiforov-Uvarov method to solve the Inverse Rosen-Morse potential. By applying this method we were able to obtain approximate solutions for the bound state energy eigenvalues and their corresponding eigenfunctions. Additionally, we graphically represented the effective potentials for several well-known DMs. We also provided numerical tables for the bound state energy levels. Notably, the results obtained in this study demonstrate excellent agreement with existing findings in the literature.

**Keywords:** Rosen-Morse potential, Nikiforov-Uvarov method, Diatomic molecules, Schrödinger equation, Approximate solution.

## SOLUTION OF THE DUFFIN-KEMMER-PETIAU EQUATION IN SNYDER-DE SITTER SPACE

M'hamed **HADJ MOUSSA**

Theoretical Physics and Radiation-Matter Interactions Laboratory (LPTHIRM), Physics Department, Sciences  
Faculty , University of Saad Dahlab-Blida 1  
PO box 270 Soumaa Road , 09000 , Blida, Algeria.  
0000-0003-3987-6790  
hadj2009@gmail.com , hadjmoussa-mhamed@univ-blida.dz

### Abstract

In this work, we present the solution of the Duffin–Kemmer–Petiau (DKP) equation in the Snyder-de Sitter (SdS) space, this equation describes the particles that have the spin is integer ( $s=0$  and  $s=1$ ). The analytical solution of the DKP equation in (SdS) space leads us to calculate the energy spectrum  $E_n$  of the particles and the corresponding wave functions  $\phi_n(x)$ , where the wave functions  $\phi_n(x)$  are given as a function of the Romanovski polynomial. Finally, the limit cases of the energy spectrum  $E_n$  are deduced.

**Keywords:** Duffin–Kemmer–Petiau Equation, Snyder-de Sitter, Energy Spectrum.

## References

- [1] M. M. Stetsko, J. Math. Phys. **56**, 012101 (2015).
- [2] R. Banerjee, K. Kumar, D. Roychowdhury, JHEP **2011**, 60 (2011).
- [3] C.B. Compean, M. Kirchbach. J. Phys. A Math. Gen. **39**, 550 (2005).
- [4] T. R. Cardoso, L. B. Castro, A. S. de Castro., J. Phys. A. Math. Theor. **43**, 055306 (2010).

# QUANTUM GRAVITY VIA TWO WHEELER-DEWITT EQUATIONS

Miloslav **ZNOJIL**

Department of Physics, Faculty of Science, University of Hradec Králové  
 Rokitsanského 62, 50003 Hradec Králové, Czech Republic  
 0000-0001-6076-0093  
 Email: znojil@ujf.cas.cz

## Abstract

A methodical analysis will be presented, devoted to certain aspects of some of the not yet resolved theoretical problems concerning a consistent quantization of gravity. Our considerations will be based on a simplified, extremely schematic cosmological model of paper [1] mimicking the unitary-evolution birth of the Universe from an initial quantum Big Bang singularity at its “proper time”  $t = 0$ .

We will argue (cf. also the more recent amendment of the model in paper [2]) that a specific realization of the Big-Bang phase transition could be rendered possible via the degeneracy of eigenvalues of a time-dependent operator  $R(t)$  representing the (in our non-covariant model, observable) space-time. This means that our “operator of geometry”  $R(t)$  (representing, in our schematic and most elementary scenario, a growing radius of the Universe) must admit a specific exceptional-point (EP) degeneracy at the EP time  $t = t^{(EP)} = 0$ .

The latter operator must have a real spectrum at  $t > 0$ . In the language of mathematics (cf. also paper [3]) this means that  $R(t)$  must be not only non-Hermitian (in any sufficiently user-friendly Hilbert space  $\mathcal{H}_{(unphysical)}$ ) but also, at the same time, self-adjoint (in a non-equivalent, properly amended Hilbert space  $\mathcal{H}_{(physical)}$ ). Thus, given  $R(t)$ , one must reconstruct a highly nontrivial physical inner-product metric  $\Theta(t)$  (cf. also a few related technical comments in paper [4]).

In the talk we will show that under these assumptions it is still possible to keep the evolution of the Universe unitary in  $\mathcal{H}_{(physical)}$  (cf. also a few illustrative, phenomenologically motivated examples in paper [5]). One must only guarantee that its theoretical description is performed using the so called non-Hermitian interaction-picture (NIP), i.e., an innovative quasi-Hermitian reformulation of the conventional quantum theory in its non-stationary version – see also all of the references [6]- [11] for various specific technical details.

In such an overall mathematical setting the construction of a non-covariant but otherwise formally internally consistent picture of physics requires that for any observ-

able  $\Lambda(t)$  of interest (i.e., e.g., for the instantaneous energy  $\Lambda_0(t) = H(t)$  of the whole Universe) we must be able to write down and solve the corresponding Heisenberg-like operator-evolution equation using a suitable Heisenberg's generator  $\Sigma(t)$  tractable, phenomenologically, as a sort of quantum Coriolis force (the most detailed account of the structure and properties of this force may be found in paper [6]).

From a purely pragmatic perspective the applicability of the theory is strongly dependent on the feasibility of the solution of the latter Heisenberg equation. In some models a perceivable simplification of this task has been achieved via certain *ad hoc* factorizations of the physical inner-product metric  $\Theta(t)$  (cf., in particular, the first proposal of such a trick in [7]).

As a consequence, even the abstract NIP approach itself acquires a richer, “hybrid theory” structure of the form outlined in papers [8] - [10]. From a more abstract conceptual perspective the existence of the latter amendment of the NIP quantum theory implies that a key advantage of its application to the non-stationary gravity is that one can simplify or even entirely circumvent the complicated explicit construction of the correct and time-dependent physical inner-product-metric operator  $\Theta(t)$ .

In the talk we will show how such a goal can be achieved by working just with the states of the Universe in a dyadic representation. This means that it is sufficient to control the kinematics by solving the mere doublet of the Schrödinger-Wheeler-DeWitt equations. In some sense the latter statement is the key message to be delivered during the talk. We may summarize that the NIP approach using two Schrödinger-Wheeler-DeWitt equations renders the conventional recommendations of the use of the time-dependent inner-product-metric operator  $\Theta(t)$  redundant.

Serendipitously one reveals that the two Schrödinger-Wheeler-DeWitt generators of the evolution of the “kinematical” state of the Universe, i.e., in our notation, the operator  $G(t)$  and its conjugate partner  $G^\dagger(t)$  *do not* have real spectra. In contrast to the rather widespread beliefs, these spectra are also practically never composed of the complex conjugate pairs. The spectrum of the above-mentioned Heisenberg's-evolution generator  $\Sigma(t)$  is also, in parallel, practically never real.

Still, one can require that the evolution of the Universe is unitary, i.e., characterized by the reality of the whole instantaneous spectrum of its observable energy. In this case an explicit information about the unitarity of the dynamics is shown to be carried by the hidden self-adjointness (i.e., by the reality of the spectrum) of the observable Hamiltonian defined by an amazingly elementary formula  $H(t) = G(t) + \Sigma(t)$ .



## References

- [1] M. Znojil, Wheeler-DeWitt equation and the applicability of crypto-Hermitian interaction representation in quantum cosmology. *Universe* **8**, 385 (2022).
- [2] M. Znojil, Quasi-Hermitian formulation of quantum mechanics using two conjugate Schroedinger equations. *Axioms* **12**, 644 (2023).
- [3] M. Znojil, Comment on 'The operational foundations of PT-symmetric and quasi-Hermitian quantum theory'. *J. Phys. A: Math. Theor.* **56**, 038001 (2023).
- [4] M. Znojil, Three alternative model-building strategies using quasi-Hermitian time-dependent observables. *Symmetry* **15**, 1596 (2023).
- [5] M. Znojil, Non-stationary non-Hermitian "wrong-sign" quantum oscillators and their meaningful physical interpretation. *Entropy* **25**, 692 (2023).
- [6] M. Znojil, Composite quantum Coriolis forces. *Mathematics* **11**, 1375 (2023).
- [7] M. Znojil, Factorized Hilbert-space metrics and non-commutative quasi-Hermitian observables. *EPL* **139**, 32001 (2022).
- [8] M. Znojil, Hybrid form of quantum theory with non-Hermitian Hamiltonians. *Phys. Lett. A* **457**, 128556 (2023).
- [9] M. Znojil, Systematics of quasi-Hermitian representations of non-Hermitian quantum models. *Ann. Phys. (NY)* **448**, 169198 (2023).
- [10] M. Znojil, Non-stationary quantum mechanics in hybrid non-Hermitian interaction representation. *Phys. Lett. A* **462**, 128655 (2023).
- [11] M. Znojil, Zig-zag-matrix algebras and solvable quasi-Hermitian quantum models. *J. Phys. A: Math. Theor.* **56**, 335301 (2023).

# POSITRON ANNIHILATION LIFETIME SPECTROSCOPY MEASUREMENTS USING Na-22 POSITRON RADIO-ISOTOPE

Mohamed Walid **HALIMI**

LPTHIRM, Department of Physics, Faculty of Science, University of Blida 1  
BP 270 Route Soumâa Blida, 09000, Algeria

Nuclear Research Centre of Algeria CRNA  
2, boulevard Frantz Fanon.Bp 399, Algiers, Algeria, 16000 Alger-Gar  
mohamed.halimi423@gmail.com

Abderrahim **GUITTOUM**

Nuclear Research Centre of Algeria CRNA  
2, boulevard Frantz Fanon.Bp 399, Algiers, Algeria, 16000 Alger-Gar

Noureddine **BENJEDDA**

Nuclear Research Centre of Algeria CRNA  
2, boulevard Frantz Fanon.Bp 399, Algiers, Algeria, 16000 Alger-Gar

Aziz **MOUZALI**

LPTHIRM, Department of Physics, Faculty of Science, University of Blida 1  
BP 270 Route Soumâa Blida, 09000, Algeria

## Abstract

In this presented work, we dive into the concepts and steps of Positron annihilation Lifetime spectroscopy ( PALS ) experimental procedures, a technique used to study materials for defects' inspection and positron lifetime in metals. The study focuses on measuring and analyzing the behavior of positrons emitted from a  $^{22}\text{NaCl}$  salt source incident upon a Kapton foil in a sandwich configuration with different materials (Si, Al, Cu, Ni, and Kapton NH500) resulting in a structure called “sandwich source” (Specimen-Kapton- $^{22}\text{NaCl}$ -Kapton-Specimen) selected to have bulk lifetimes sufficiently distinct from the lifetime of the positron source. This selection allowed us to investigate the unique contribution of each material to the annihilation process. The lifetimes and relative intensities of annihilating positrons are measured and compared, revealing the dependence of source contribution on the atomic number (Z) and density of the traversed material. The work presents the main steps of this procedure at room temperature, the two-state Conventional Model (CM) as the best and efficient fitting approach for results used by LT (Lifetime Toolkit) ver 9.2 including  $^{22}\text{Na}$  contributions

and different elements in the sample, to be identified and quantified. Understanding PALS measurement system and the role of the electronic equipment and its beneficial for the analysis of PALS results and how it affects the source count rate is presented.

**Keywords:** Positron annihilation spectroscopy; positron source; positron lifetime; Na-22 source contribution; Source Correction.

# SHELL-MODEL STUDY OF THE SPECTROSCOPIC PROPERTIES OF THE $^{26}\text{Mg}$ AND $^{26}\text{Si}$ MIRRORS

Mouna **BOUHELAL**

LPAT, Echahid Cheikh Larbi Tebessi University  
Route de Constantine, 12002, Tebessa, Algeria  
0000-0001-7346-9801  
mouna.bouhelal@univ-tebessa.dz or m.bouhelal@yahoo.fr

Abir **SELIM**

LPAT, Echahid Cheikh Larbi Tebessi University  
Route de Constantine, 12002, Tebessa, Algeria  
abirslm95@gmail.com

Florent **HAAS**

IPHC, CNRS/IN2P3, Université de Strasbourg  
F-67037 Strasbourg, Cedex2, France

## Abstract

The sd shell nuclei exhibit very different structural properties ranging from nuclei near the stability-line to those deficient or rich of neutrons. Additionally, the neutron-deficient side is of great relevance in astrophysics, especially the rapid proton capture rp-process [1]. Advances in spectroscopic studies of these nuclei have aroused renewed interest. One of the most important rp-process is the  $^{25}\text{Al}(p\gamma)^{26}\text{Si}$  reaction. The determination of the correct levels of  $^{26}\text{Si}$ , based on their analogues in the mirror nucleus  $^{26}\text{Mg}$ , is crucial to calculate the reaction rate. The spectroscopic properties, energy spectrum up to about 10 MeV and electromagnetic transition properties of  $^{26}\text{Mg}$  are comprehensively studied in a shell model context. These properties are quantitatively reproduced using the effective  $(0+1)\hbar\omega$  PSDPF interaction [2]. The comparison of the obtained results with available experimental data [3] led to the confirmation of the ambiguous states and to the prediction of the spin/parity assignments of the unknown states. Detailed discussion of this study will be presented in our contribution.

## References

- [1] A. Wendt et al, Phys. Rev. C **90**, 054301 (2014).
- [2] M. Bouhelal et al, Nucl. Phys. A **864**, 113 (2011).

[3] <http://www.nndc.bnl.gov/nudat2>.

## A STUDY OF THE MOTION OF BOSON PARTICLES WITH INTERACTION IN THE COSMIC STRING SPACE TIME

Moussa **ABBAD**

Laboratory of Applied and Theoretical Physics, Echahid Cheikh Larbi Tébessi University, Tebessa, Algeria  
moussa.abbad@univ-tebessa.dz

Houcine **AOUNNALLAH**

Department of Science and Technology, Echahid Cheikh Larbi Tébessi University, Tebessa, Algeria  
Houcine.Aounallah@univ-tebessa.dz

### Abstract

In this work, we study scalar bosons with vector potentials in a cosmic string space-time background. We choose DKP equation spin 0 with a position-dependent mass via transformation  $m \rightarrow (m + S(r))$  for three different types of potential, such as linear type and Coulomb type and we obtain a second-order differential equation known as the hypergeometric and the corresponding confluent Heun function. Finally, we solve the wave equation by the Frobenius method as a power series expansion around the origin and obtain the energy levels and the wave function.

### References

- [1] A. Boumali and H. Aounallah, Adv. High Energy Phys. **2018**, 1031763 2018.
- [2] H. Aounallah and A. Boumali , Phys. Part. Nucl . Lett . **16**, 195 (2019).
- [3] A. Boumali and H. Aounallah , Rev. Mex. Fis . **66**(2), 192 (2020).

## EUP EFFECTS ON 3D DKP OSCILLATOR

Mustafa **MOUMNI**

LabPRIM, Faculty of Matter Sciences, University of Batna1  
 Allees 19 mai, Route de Biskra, 05000, Batna, Algeria  
 0000-0002-8096-6280  
 m.moumni@univ-batna.dz

Mokhtar **FALEK**

Department Physics, Faculty of Sciences, University of Khenchela  
 BP 1252 Road of Batna, 40004, Khenchela, Algeria  
 0000-0002-0466-9559  
 falekmokhtar75@gmail.com

Mahmoud **MERAD**

Department Physics, Faculty of Sciences, University of Oum el Bouaghi  
 B.P 358 route de constantine, 04000, Oum el Bouaghi, Algeria  
 0000-0001-7547-6933  
 meradm@gmail.com

### Abstract

We present the exact solutions for the three-dimensional Duffin-Kemmer-Petiau equation for both spin 0 and spin 1 particles in the field of a harmonic oscillator potential, while considering the presence of minimal uncertainty in momentum within the anti-de Sitter model. We use the representation of vector spherical harmonics for the wave-functions and the Nikiforov-Uvarov method to precisely determine analytical expressions of the energy eigen-values and the wave eigen-functions for both scalar and vector cases. Our analysis of the energy spectrum leads to a new interpretation of the correspondence principal between classical and quantum systems and a new formulation of natural and unnatural vector states.

### References

- [1] S. Mignemi, Mod. Phys. Lett. A **25**, 1697 (2010).
- [2] B. Hamil and M. Merad, Eur. Phys. J. Plus **133**, 174 (2018).
- [3] B. Hamil, M. Merad and T. Birkandan, Eur. Phys. J. Plus **134**, 278 (2019).

- [4] Y. Nedjadi and R.C. Barrett, J. Phys. A **27**, 4301 (1994).
- [5] A.F. Nikiforov and V.B. Uvarov, Special Functions of Mathematical Physics (Birkhauser, Basel, 1988)



## CALCULATION OF SELF INDUCTANCE OF A FINITE COIL

Muzaffer **ERDOGAN**

Tekirdag Namik Kemal University, Tekirdag, Turkey

0000-0001-8738-2299

merdogan@nku.edu.tr

### Abstract

This study focuses on the calculation of self-inductance of a coil. The magnetic field generated by a current passing through a single turn is first expressed as a Taylor series expansion in terms of powers of the distance from the center of the turn. Subsequently, the magnetic field at the points off axis, is computed as a linear serial combination of Legendre polynomials. By integrating the component of this magnetic field parallel to the axis, the magnetic flux produced by one turn in another turn is determined. This result is then utilized to obtain the total magnetic flux passing through all turns. The total magnetic flux is equated to  $L I$ , where  $L$  represents the self-inductance of the coil, and  $I$  is the current passing through it. This equation allows for the direct calculation of the self-inductance.

## EXPLORING THE EFFECT OF GUP ON SCATTERING OF SCHWARZCHILD BLACK HOLE

Narges **HEIDARI**

Physics Department, Shahrood University of Technology  
Shahrood, Iran  
0000-0002-4623-8909  
heidari.n@gmail.com

Hassan **HASSANABADI**

Physics Department, Shahrood University of Technology  
Shahrood, Iran  
hha1349@gmail.com

Hao **CHEN**

School of Physics and Electronic Science, Zunyi Normal University  
Zunyi, China  
haochen1249@yeah.net

### Abstract

This work examines the quantum correction of the Schwarzschild black hole metric using the generalized uncertainty principle (GUP). We consider a massless scalar field, explore the associated effective potential and calculate the GUP-corrected reflection and transmission coefficients of the scattered radial wave function using the Pösch-Teller method. Our findings provide insights into the behavior of these coefficients under GUP corrections, which can deepen our understanding of black hole physics.

## NANOCRYSTALLINE NiTi ALLOYS PRODUCED BY COLD ROLLING IN THE MARTENSITIC STATE

Paweł **ŚWIEC**

Institute of Material Science  
75 Pułku Piechoty 1a Street, 41-500 Chorzów, Poland pawel.swiec@us.edu.pl

Maciej **ZUBKO**

Institute of Material Science  
75 Pułku Piechoty 1a Street, 41-500 Chorzów, Poland

Danuta **STROZ**

Institute of Material Science  
75 Pułku Piechoty 1a Street, 41-500 Chorzów, Poland

Karsten **GLOWKA**

Institute of Material Science  
75 Pułku Piechoty 1a Street, 41-500 Chorzów, Poland

### Abstract

Near equiatomic NiTi alloys exhibit unique properties of shape memory (SME) and superelasticity (SE) caused by reversible thermoelastic martensitic transformation. Additionally, due to the high content of Ti, which leads to the formation of a passive layer on the material surface of this alloy, these alloys exhibit high corrosion resistance and biocompatibility [1]. Because of these unusual properties, NiTi alloys are widely used in medicine as implants in orthopaedic surgery. In recent years, severe plastic deformation (SPD) has drawn more attention due to the possibility of forming nanostructures in bulk metals and alloys [2]. This process relies on material amorphisation caused by large plastic deformation and further annealing in order to cause recrystallisation and grain growth of the deformed structure. It was shown that nanostructured materials own increased yield strength and ductility. Moreover, nanostructured Ti shows better corrosion resistance and cytocompatibility, which are important features in medicine and implantology [3]. In present studies, the Ni-49.3 % at.Ti alloy in the form of 3.5 mm wire, characterised by temperatures  $M_f -11.5\text{ }^{\circ}\text{C}$  and  $A_f 52.1\text{ }^{\circ}\text{C}$ , was subjected to

SPD by cryo-rolling in the martensitic state. To maintain the material at a reduced temperature, it was cooled in a liquid nitrogen batch after each pass. After deformation, the obtained materials were annealed at 350, 400 and 450 °C for 15, 60 and 240 minutes without a protective atmosphere and quenched in ice-cold water. Transmission electron microscopy (TEM) observation was carried out to investigate structure changes. The received material exhibited an unusual course of martensitic transformation, which was examined by in situ heating X-ray diffraction (XRD) method and differential scanning calorimetry (DSC), which the non-homogenous structure of cold-rolled alloy might cause. Additionally, recrystallisation and grain growth kinetics were investigated.

## References

- [1] K. Otsuka, X. Ren, Prog. Mater. Sci. **50**, 511–678 (2005). doi:10.1016/j.pmatsci.2004.10.001.
- [2] R. Z. Valiev, I. V. Alexandrov, Nanostructured Mater. **12**, 35–40 (1999). doi:10.1016/S0965-9773(99)00061-6.
- [3] R. Z. Valiev, I. P. Semenova, V. V. Latysh, H. Rack, T. C. Lowe, J. Petruzella, L. Dluhos, D. Hrusak, J. Sochova, Adv. Eng. Mater. **10**, 15–17 (2008). doi:10.1002/adem.200800026.
- [4] E. Ryklina, S. Prokoshkin, K. Vachyan, IOP Conf. Ser. Mater. Sci. Eng. **63**, 012110 (2014). doi:10.1088/1757-899X/63/1/012110.
- [5] A. Ahadi, Q. Sun, Appl. Phys. Lett. **103**, 021902 (2013). doi:10.1063/1.4812643.
- [6] S. Jiang, L. Hu, Y. Zhao, Y. Zhang, Y. Liang, Mater. Sci. Eng. A. **569**, 117–123 (2013). doi:10.1016/j.msea.2013.01.058.

# BUMBLEBEE BLACK HOLES SURROUNDED BY DARK MATTER SPIKE

Soroush **ZARE**

Faculty of Physics, Shahrood University of Technology  
3619995161-316, Shahrood, Iran  
soroushzrg@gmail.com

Hassan **HASSANABADI**

Faculty of Physics, Shahrood University of Technology  
3619995161-316, Shahrood, Iran  
0000-0001-7487-6898  
hha1349@gmail.com

## Abstract

We explore the impact of dark matter spike in the vicinity of the supermassive black hole at the center of the M87 galaxy within the context of Bumblebee Gravity, a framework for gravitational physics. Our primary goal is to assess how the background characterized by spontaneous Lorentz symmetry breaking affects the characteristics of the horizon, ergoregion, and shadow of the Kerr Bumblebee black hole in the spike region. To achieve this, we initially introduce the distribution of dark matter into a Lorentz-violating spherically symmetric space-time, treating it as part of the energy-momentum tensors within Einstein's field equations. This process yields a space-time metric describing a Schwarzschild Bumblebee black hole with dark matter distribution in the spike region and beyond. Subsequently, we extend this solution to encompass a Kerr Bumblebee black hole, employing the Newman-Janis-Azreg-Ainou algorithm. We then consider observational data concerning the density and radius of the dark matter spike, as well as the Schwarzschild radius of the supermassive black hole in the M87 galaxy. Using this information, we analyze the shapes of shadows and illustrate how the spin parameter, the Lorentz-violating parameter, and the corresponding parameters of the dark matter halo influence the deformation and size of the shadow.

## References

- [1] S. Capozziello, S. Zare, D. F. Mota and H. Hassanabadi, J. Cosmol. Astropart. Phys. **05**, 027 (2023).

- [2] S. Nampalliwar, S. Kumar, K. Jusufi, Q. Wu, M. Jamil and P. Salucci, *Astrophys. J.* **916**, 116 (2021).
- [3] Z. Xu, J. Wang and M. Tang, *J. Cosmol. Astropart. Phys.* **09**, 007 (2021).

## HOW TO CALCULATE BLACK HOLE SHADOW

E. Ulaş **SAKA**

Department of Physics, Istanbul University, Istanbul Turkey

0000-0001-5531-9252

ulassaka@istanbul.edu.tr

### Abstract

In this talk, we present an analytical calculation scheme of black hole shadows in various cases. First, we give the definition of the shadow of a black hole then we present its relation with the critical parameters. We explain how to derive the angular size of the shadow for an observer at any distance from the black hole and we calculate the shadow of Kerr black hole for an observer at large distance. Finally, we discuss the deformation of the shadow of the Kerr black hole when it is surrounded by matter in different profiles.

## SOLITON SOLUTION OF GROSS-PITAEVSKII EQUATION

Zeyneb **TAIBI**

Laboratory for Theoretical Physics and Material Physics Faculty of Exact Sciences and Informatics,  
Hassiba Benbouali University of Chlef, Chlef, 02000 Algeria [physique2tz@gmail.com](mailto:physique2tz@gmail.com)

Houria **CHAACHOUA SAMEUT**

Laboratory for Theoretical Physics and Material Physics Faculty of Exact Sciences and Informatics,  
Hassiba Benbouali University of Chlef, Chlef, 02000 Algeria  
[chachou-houria@yahoo.fr](mailto:chachou-houria@yahoo.fr)

Halima **BELKROUKRA**

Laboratory for Theoretical Physics and Material Physics Faculty of Exact Sciences and Informatics,  
Hassiba Benbouali University of Chlef, Chlef, 02000 Algeria  
[h.belkroukra@univ-chlef.dz](mailto:h.belkroukra@univ-chlef.dz)

### Abstract

The Gross-Pitaevskii equation describes Bose-Einstein condensates in the low-temperature regime. We drive analytical solutions of nonlinear equations by applying the Lax pair and Darboux transformation to find the solution as form soliton and its subsequent in optical fiber, quantum gases, hydrodynamics, and plasma, etc.

**Keywords:** Darboux transformation, Lax Pair, Soliton and Gross- Pitaevskii equation.



## EXPANSION A 3D DIPOLAR BEC IN RANDOM POTENTIALS

Zohra **MEHRI**

Department of Physics, Faculty of Sciences and Technology, Ahmed Zabana University of Relizane Bourmadia, BP  
48000, Relizane, Algeria  
zohra.mehri@univ-relizane.dz

Abdelaali **BOUDJEMAA**

Department of Physics, Faculty of Exact Sciences and Informatics, Hassiba Benbouali University of Chlef P.O. Box  
78, 02000, Ouled-Fares, Chlef, Algeria.  
a.boudjemaa@univ-chlef.dz

### Abstract

We study the effects of dipole-dipole interaction on the diffusion of an expanding atomic Bose-Einstein condensate with tunable s-wave interactions in a three-dimensional disorder potential. First-order correction due to local and nonlocal nonlinearities to the average atomic density is analytically calculated in the long expanding time limit using a perturbative theory. It is found that the diffusion coefficient exhibits a stronger anisotropy-dependence due to the dipolar interactions. We show that the intriguing interplay of dipolar and nondipolar interactions and disorder potential may affect the diffusive expansion.

### References

- [1] A. Aspect and M. Inguscio, Phys. Today **62**, 30 (2009).
- [2] A. Boudjemaa, Phys. Lett. A **379**, 2484 (2015).
- [3] A. Boudjemaa, J. Phys. B: At. Mol. Opt. Phys. **49**, 105301 (2016).
- [4] A. Boudjemaa, Phys. Lett. A **424**, 127867 (2022).
- [5] A. Boudjemaa, Eur. Phys. J. B **92**, 145 (2019).